



Flat Band Structures

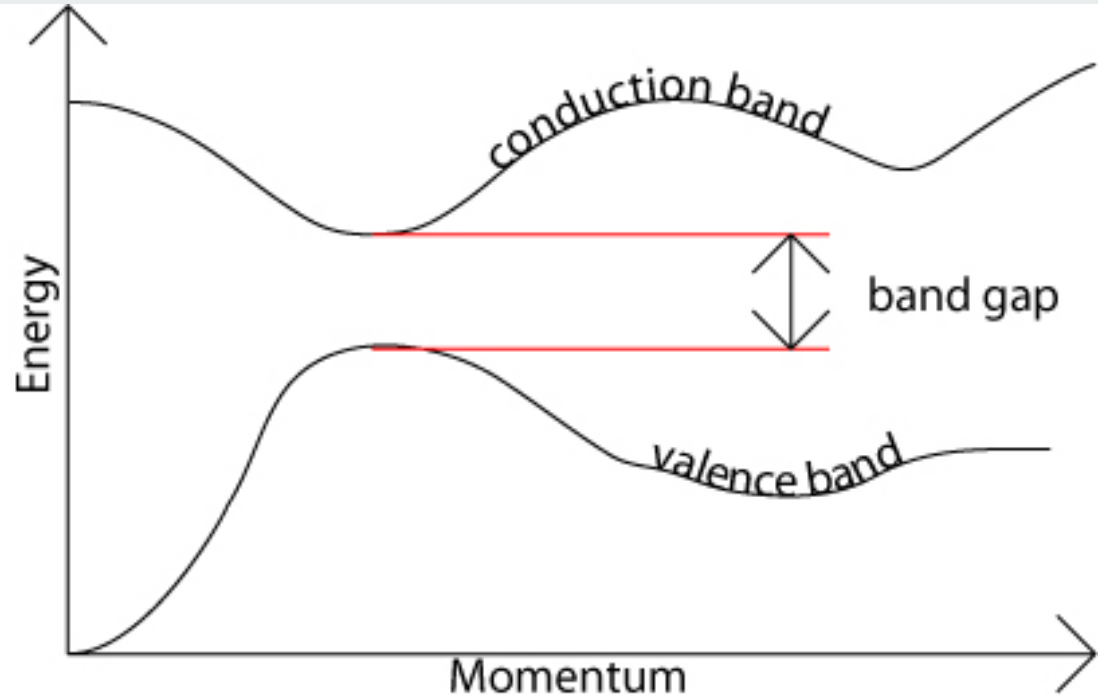
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Condensed Matter Physics at OU In Collaboration with Dr. Bruno Uchoa

What are Flat Bands



- Flat bands are states in which energy is independent of momentum.
 - Group velocity is zero
- Generally unstable
 - Susceptible to perturbations
- Leads to phenomena such as ferromagnetism, superconductivity, and superfluidity as seen in CuO_2



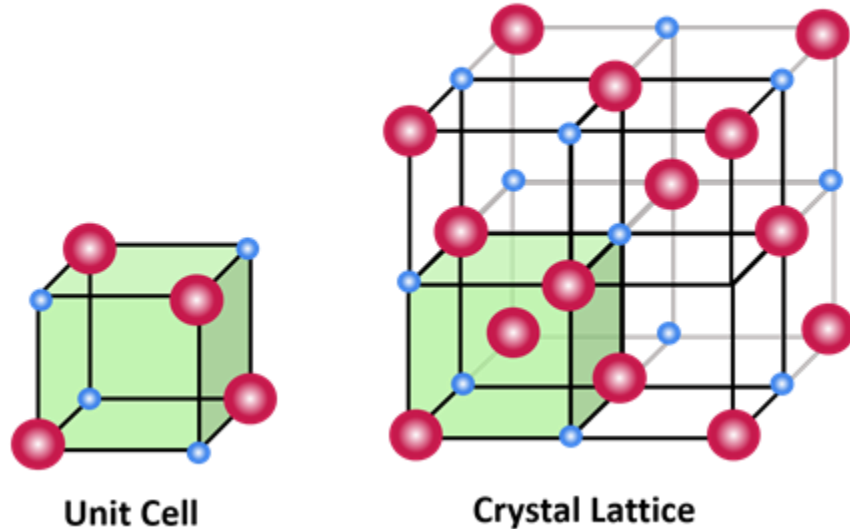
Lattices

Occured in twisted bilayer graphene

- Attempts to make flat band lattices have
 - Used origami rules and fractals
- The edge states are different from the bulk
 - Chiral edge states

$$\psi_{n\vec{k}}(\vec{r}) = e^{i\vec{k}\cdot\vec{r}} u_{n\vec{k}}(\vec{r})$$

Crystal Lattice and Unit Cell



Relation to Anomalous Quantum Hall Effect

- The Original Quantum Hall Effect was shown using a magnetic field
 - First example of a topological insulator
 - Conductivity was quantized $\sigma = C$ (e^2/h)
 - C here is the chern number, dependent on the topology of the band structure
- The AQHE was demonstrated without the use of an external magnetic field
 - Due to spin-orbit coupling (SOC)

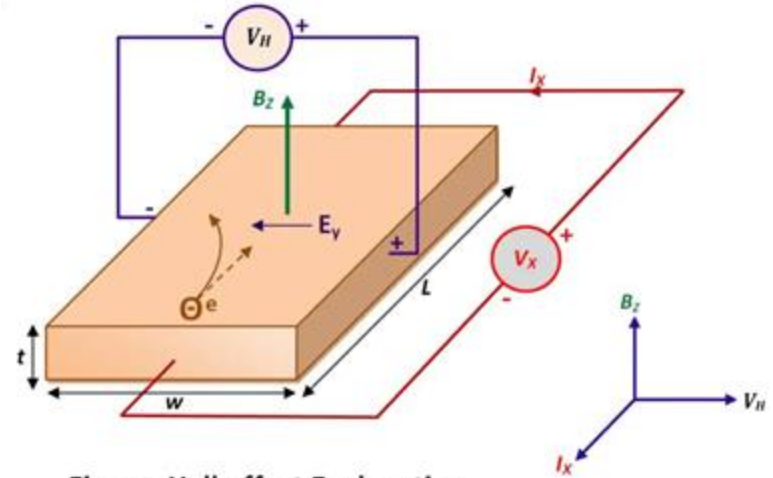


Figure- Hall effect Explanation

What I Will Be Researching

Calculations on

- The Chern number using the Berry curvatures of different materials
- Hall conductivity
- Polarization using the Berry phase
- Orbital Magnetization using Wannier functions

□ All these relate to topology

Berry Connections and Berry Curvature

- Berry's Connection

$$A_n(R) = i \langle n(R) | \nabla_R | n(R) \rangle$$

- Berry's Curvature

$$'B' = \nabla_R \times A_n(R)$$

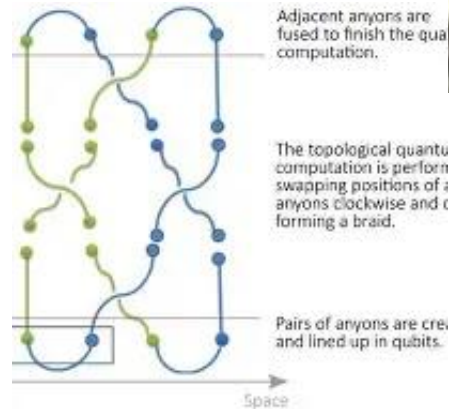
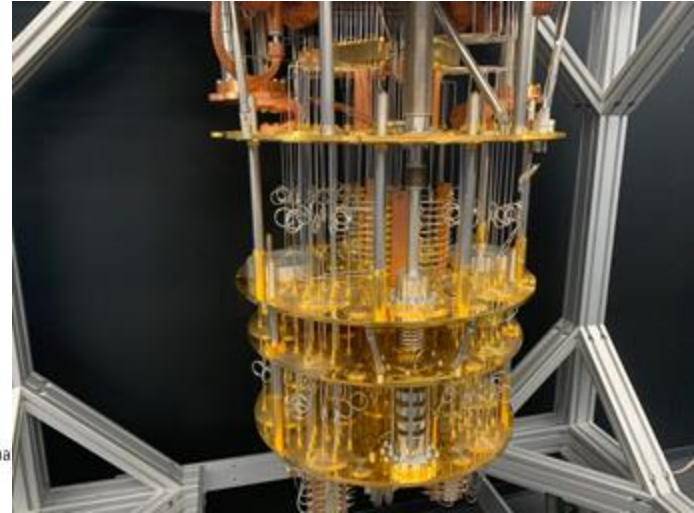
- Berry's Phase

$$\gamma_n(T) = i \oint A_n(R) \cdot dR$$

$$\begin{aligned} \Phi &= \int_S B \cdot da \\ B &= \nabla \times A \\ \Phi &= \int_S (\nabla \times A) \cdot da = \oint_C A \cdot dr \\ \gamma_n(T) &= i \oint \langle \psi_n | \nabla_R \psi_n \rangle \cdot dR \end{aligned}$$

Significance of Topological Flat Bands

- Would significantly improve topological quantum computing
 - Information is encoded differently from qubits through anyons
 - Improved coherence times
- Studying correlation electron physics
 - e. g. Mott insulators



Adjacent anyons are fused to finish the quantum computation.

The topological quantum computation is performed by swapping positions of anyons clockwise and counter-clockwise, forming a braid.

Pairs of anyons are created and lined up in qubits.

Questions?



Works Cited



[Crystal Lattice — Structure & Formation - Expii](#)

<https://www.slideserve.com/michaelbrooks/chapter-18-electrical-properties-powerpoint-ppt-presentation>

[1308.0343](#)

[Observation of topological surface state quantum Hall effect in an intrinsic three-dimensional topological insulator](#)