

Eddre? / Herry?
PROBLEM 4

a) (3 points) Imagine a large cloud of pure interstellar hydrogen having density n atoms/cm³. Φ is the number of photons emitted by a star per second which are capable of photoionizing neutral hydrogen ($\lambda < 912\text{\AA}$), while αn^2 is the number of recombinations per second per cm³. If each photon results in a photoionization and the rate of photoionization equals the rate of recombination, find an expression for the Strömgren sphere R_s , i.e. the radius of the ionized gas cloud, in terms of n , Φ , and α .

b) (2 points) Find R_s in parsecs for an O star if $\Phi = 10^{49}$ photons/s, $n = 10$ atoms/cm³, and $\alpha = 2 \times 10^{-13}$.

c) (2 points) Find R_s in parsecs for the sun if $\Phi = 5 \times 10^{23}$ photons/s, while n and α remain the same.

d) (3 points) Could the cloud around the sun be seen by an astronomer on α -Centauri (distance=1.31pc) using a telescope which can just barely resolve objects which are 1" in angular size?

Constants:

$$1 \text{ parsec} = 3.086 \times 10^{18} \text{ cm}$$

$$1 \text{ radian} = 206265 \text{ arcsec}$$

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Astro #4

a) $[n] = \frac{\text{atoms}}{\text{cm}^3}$

$$[\Phi] = \frac{\text{photons}}{\text{s}}$$

* Assuming # of ionizations and recombinations are the same over a 1s interval

$$\Phi = \int \alpha n^2 dV$$

$$\Phi = \alpha n^2 \frac{4}{3} \pi r^3$$

$$\left(\frac{3\Phi}{4\alpha n^2 \pi} \right)^{1/3} = r$$

b)
$$r = \left(\frac{3 \cdot 10^{49} \frac{1}{\text{s}}}{\pi \cdot 4 \cdot 2 \cdot 10^{-13} (10 \frac{\text{cm}^2}{\text{s}})^2} \right)^{1/3}$$

$$= 4.92 \cdot 10^{14} \text{ cm}$$

$$\approx 15.96 \text{ pc}$$

c)
$$r = \left(\frac{5 \cdot 10^{23}}{\pi \cdot 4 \cdot 2 \cdot 10^{-13} \cdot 10^2 \frac{1}{\text{cm}^3}} \right)^{1/3}$$

$$= 1.258 \cdot 10^{11} \text{ cm}$$

$$= 4.08 \cdot 10^{-8} \text{ pc}$$