

$$v_f^2 = v_i^2 + 2a(x_f - x_i)$$

$$v^2 = 0 + 2(-g)(-h)$$

$$v^2 = 2gh$$

$$v = \sqrt{2gh}$$

choosing zero of coordinate system at bottom of fall
choosing positive x direction up.

$$x_i = h$$

$$x_f = 0$$

$$v_i = 0$$

$$v_f = v \text{ (unknown)}$$

$$a = -g$$

$$t_i = 0$$

$$t_f = t \text{ (unknown)}$$

choose negative square root because of coordinate system choice.

speed = $\sqrt{2gh}$ ← useful to remember

② Simply the reverse of the above problem.

$$x_i = 0$$

$$x_f = h \text{ (unknown)}$$

$$v_i = v_0$$

$$v_f = 0 \text{ (at rest)}$$

$$a = -g$$

$$t_i = 0$$

$$t_f = t$$

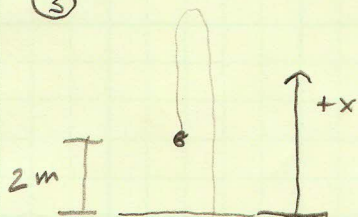
$$v_f^2 = v_i^2 + 2a(x_f - x_i)$$

$$0 = v_0^2 + 2(-g)(h - 0)$$

$$2gh = v_0^2 \Rightarrow h = \frac{v_0^2}{2g}$$

also useful to know.

③



throw up, how long until it comes down
choose zero of C.S. at bottom
choose +x up

$$t_i = 0 \leftarrow \text{point of launch}$$

$$t_f = t \leftarrow \text{time it hits ground.}$$

$$x_i = 1.5$$

$$x_f = 0$$

$$v_i = 19$$

$$v_f = 0$$

$$a = -g$$

$$t_i = 0$$

$$t_f = t$$

$$\Delta t = t$$

$$x_f = x_i + v_i t + \frac{1}{2} a t^2$$

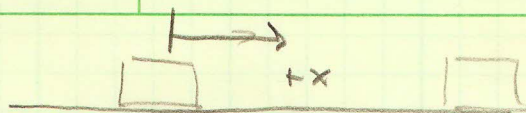
$$0 = 1.5 + 19t - 4.9t^2$$

$$t = \frac{-19 \pm \sqrt{19^2 - (4)(-4.9)(1.5)}}{-9.8} = \frac{-19 \pm 19.759}{-9.8}$$

must choose neg. square root for $t \geq 0$

$$t = \frac{-38.759}{-9.8} = \underline{\underline{3.95 \text{ sec}}}$$

④



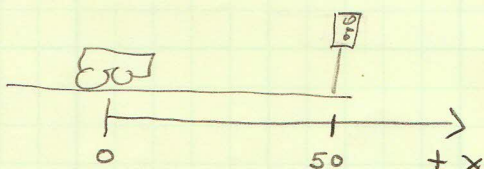
$$\begin{aligned} v_i &= 3.2 \text{ m/s} \\ v_f &= 0 \\ a &= -0.6 \text{ m/s}^2 \quad (\text{slowing down}) \end{aligned}$$

$$\begin{aligned} t_i &= 0 \\ t_f &= t \\ \Delta t &= t \end{aligned}$$

$$v_f = v_i + a \Delta t$$

$$0 = 3.2 + (-0.6)(t) \quad t = \frac{3.2}{.6} = \underline{5.33 \text{ sec}}$$

⑤



$$\begin{aligned} x_i &= 0 \\ x_f &= 50 \\ v_i &= 20 \\ v_f &= v \\ a &= 5 \\ t_i &= 0 \\ t_f &= t \end{aligned}$$

$$v_f^2 = v_i^2 + 2a \Delta x$$

$$v_f^2 = 20^2 + (2)(5)(50) = 900$$

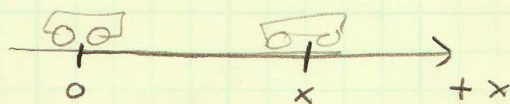
$$\underline{v_f = 30 \text{ m/s}} \quad \text{choose + square root}$$

$$v_f = v_i + at$$

$$\Delta t = t$$

$$30 = 20 + 5t \rightarrow \underline{t = 2 \text{ sec}}$$

⑥



$$\begin{aligned} x_i &= 0 \\ x_f &= x \quad (\text{unknown}) \\ v_i &= 30 \\ v_f &= v \quad (\text{unknown}) \\ a &= -20 \quad (\text{given a.s.}) \\ t_i &= 0 \\ t_f &= 1.3 \end{aligned}$$

$$\Delta t = t_f - t_i$$

$$x_f = x_i + v_i \Delta t + \frac{1}{2} a \Delta t^2$$

$$\begin{aligned} x &= 0 + (30)(1.3) + \frac{1}{2}(-20)(1.3)^2 \\ &= 39 - 16.9 = \underline{22.1 \text{ m}} \end{aligned}$$

$$v_f = v_i + a \Delta t$$

$$v = 30 + (-20)(1.3)$$

$$= 30 - 26 = \underline{4 \text{ m/s}}$$