

ND READING Assignment

makeup exam 3-6 today in my
office (show up by 5)

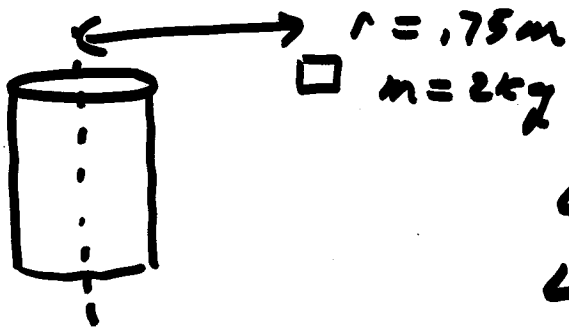
Pre Dental Club Last mtg of
semester

Dale Hall 103

Thursday at 6:30

Free food from Chili's

EX) A student is sitting on a swivel seat and holding a 2kg mass in each hand. He is rotating at 1 rev/s when arms outstretched .75 m from axis of rotation. What happens when he pulls in arms. Person can be approximated as a cylinder of mass 72kg and radius .25 m.



Conserve angular momentum

$$\sum L_i = \sum L_f$$

$$L_i = I_B \omega_i + 2 I_m \omega_i$$

$$L_f = I_B \omega_f + 0 \quad \begin{matrix} r=0 \\ I=0 \end{matrix}$$

$$(I_B + 2 I_m) \omega_i = I_B \omega_f$$

$$I = \frac{1}{2} M R^2$$

$$\left(\frac{1}{2} M R^2 + 2 \cdot m r^2 \right) \omega_i = \frac{1}{2} M R^2 \omega_f$$

$$\omega_f = \left(\frac{\frac{1}{2} M R^2 + 2 m r^2}{\frac{1}{2} M R^2} \right) \omega_i$$

$$\omega_f = \left(\frac{\frac{1}{2} (72 \text{ kg} \times .25 \text{ m})^2 + 2 \cdot (2 \text{ kg} \times .75 \text{ m})^2}{\frac{1}{2} (72 \text{ kg} \times .25 \text{ m})^2} \right) \cdot 1 \text{ rev/s}$$

$$\omega_f = 2 \text{ rev/s}$$

Equilibrium

object at rest is an example

Forces are balanced so no

acceleration and no angular acceleration

→ Constant velocity ($\vec{v}=0$)

→ Constant angular velocity ($\omega=0$)

If an object is not moving ($\vec{v}=0$) / rotating ($\omega=0$) it is in equilibrium

$$\rightarrow \Sigma \vec{F} = m\vec{a} \quad \Sigma \tau = I\alpha$$

$$\vec{a}=0 \quad \alpha=0$$

$$\Sigma \vec{F} = 0 \quad (\text{Done this before})$$

$$\Sigma \tau = 0 \quad (\text{new})$$

$$\Sigma \tau = \Sigma r F \sin \theta = 0$$

Note Torque can be measured relative to any axis

ex) A uniform 40 N Board supports 2 children weighing 500 N and 350 N. A support is under center of mass of board. The 500 N child is 1.5 m from center.

- a) what is Force That support exerts
b) where should 350 N child sit to balance board?



$$\sum F_y = 0$$

$$F_N - 500\text{ N} - 40\text{ N} - 350\text{ N} = 0$$

$$F_N = 890\text{ N}$$

$$\Sigma \tau = 0$$

Choose support as axis

$$+ (500\text{N} \cdot 1.5\text{m}) \cdot \sin 90^\circ$$

$$0 \quad (\text{support}) \quad r = 0$$

$$- (350\text{N} \cdot r) \sin 90^\circ = 0$$

$$500\text{N} \cdot 1.5\text{m} - 350\text{N} \cdot r = 0$$

$$r = 2.14\text{m from support}$$

Choose 500N child as axis

$$\Sigma \tau = 0$$

$$0 \quad 500\text{N child} \quad r = 0$$

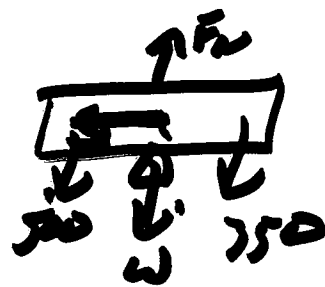
$$- 40\text{N} \cdot 1.5\text{m} \cdot \sin 90^\circ$$

$$- 350\text{N} \cdot r \cdot \sin 90^\circ$$

$$+ 890\text{N} \cdot 1.5\text{m} \cdot \sin 90^\circ = 0$$

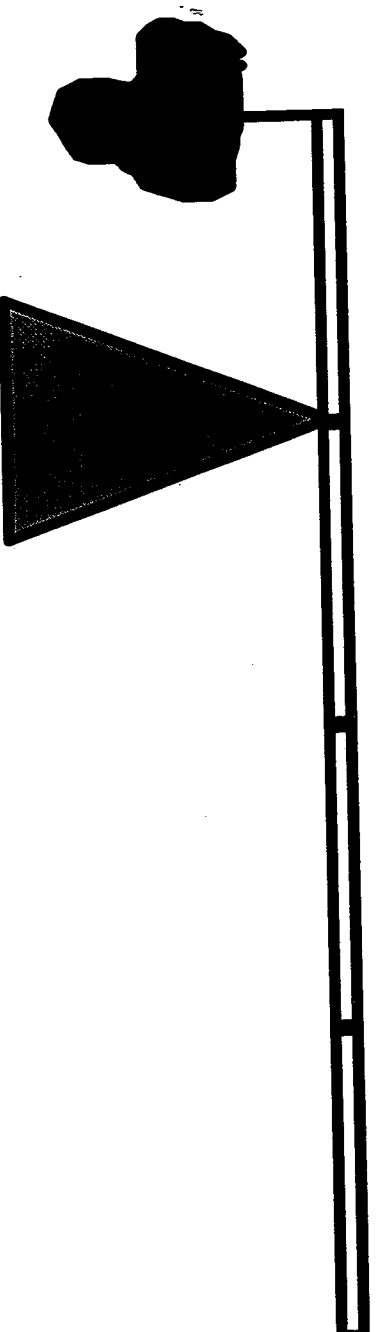
$$r = 3.64\text{m from 500N child}$$

$$3.64 - 1.5\text{m} = 2.14\text{m from support}$$



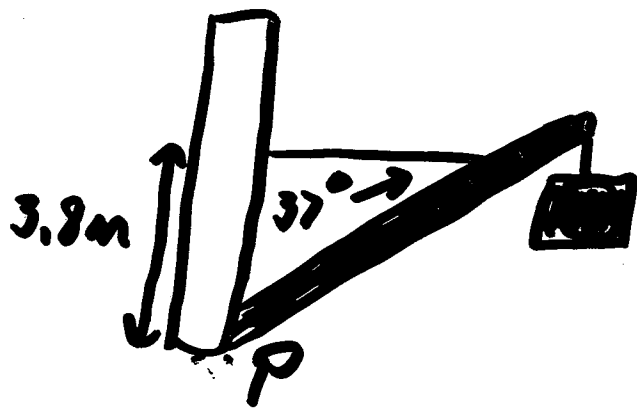
Interactive Question

A 1-kg rock is suspended by a massless string from one end of a 1-m measuring stick. What is the weight of the measuring stick if it is balanced by a support force at the 0.25-m mark?



- A) 0.25 kg
- B) 0.5 kg
- C) 1 kg
- D) 2 kg
- E) 3 kg

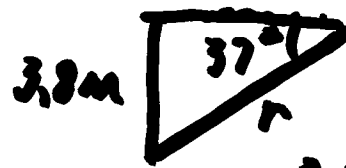
EX) A Traffic light hangs as shown



Pole 7.5m long (L)
Pole mass 8.0kg (M)
light mass 11kg (m)

Determine Tension in cable and
Vertical and horizontal components
of force on the pivot point P

F.O.O



$$\sin 37^\circ = \frac{3.8m}{r}$$

$$3.8m = r \sin 37^\circ$$

$$\sum \tau = 0$$

$$-Mg\left(\frac{L}{2}\right) \sin 53^\circ - mgL \sin 53^\circ + \frac{Tr \sin 37^\circ}{3.8m} = 0$$

$$\boxed{T = 230N}$$

$$\sum F_x = 0$$

$$F_x - T = 0 \quad F_x = T \quad \boxed{230N}$$

$$\sum F_y = 0$$

$$F_y - Mg - mg = 0$$

$$F_y = Mg + mg = \boxed{170N}$$