

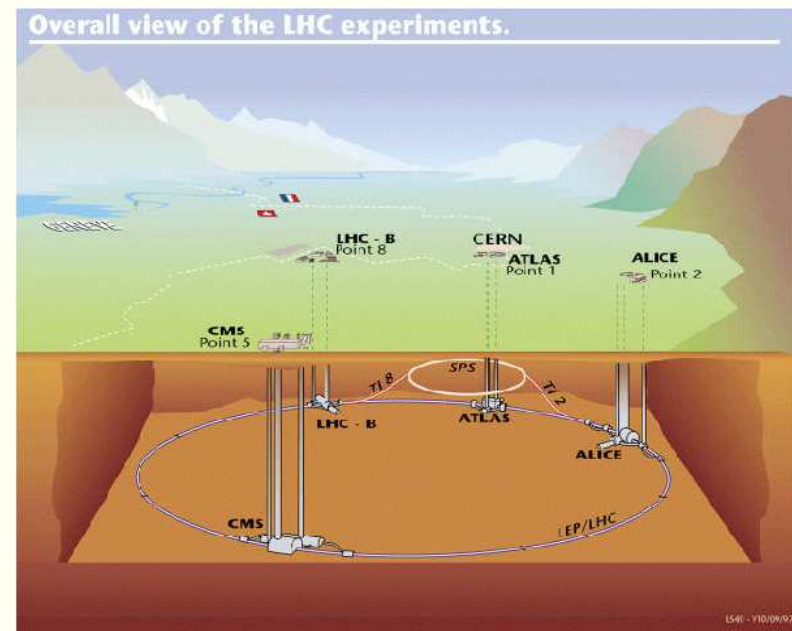
Supersymmetric Dark Matter: Direct, Indirect and Collider Searches

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OUTLINE

- ★ The Standard Model
- ★ Inconsistencies
- ★ Supersymmetry
- ★ Dark matter (DM)
 - neutralino, axion/axino, gravitino
- ★ The Hunt for DM at LHC
- ★ direct DM searches
- ★ indirect DM searches



The Standard Model of Particle Physics

- ★ gauge symmetry: $SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow g, W^\pm, Z^0, \gamma$
- ★ matter content: 3 generations quarks and leptons

$$\begin{pmatrix} u \\ d \end{pmatrix}_L, u_R, d_R; \begin{pmatrix} \nu \\ e \end{pmatrix}_L, e_R \quad (1)$$

- ★ Higgs sector \Rightarrow spontaneous electroweak symmetry breaking:

$$\phi = \begin{pmatrix} \phi^+ \\ \phi_0 \end{pmatrix} \quad (2)$$

- ★ \Rightarrow massive W^\pm, Z^0 , quarks and leptons
- ★ $\mathcal{L} = \mathcal{L}_{gauge} + \mathcal{L}_{matter} + \mathcal{L}_{Yuk.} + \mathcal{L}_{Higgs}$: 19 parameters
- ★ good-to-excellent description of (almost) *all* accelerator data!

Shortcomings of SM

Data

- ★ neutrino masses and mixing
- ★ baryogenesis (matter anti-matter asymmetry)
- ★ cold dark matter
- ★ dark energy

Theory

- ★ quadratic divergences in scalar sector \Rightarrow fine-tuning
- ★ origin of generations
- ★ explanation of masses/ mixing angles
- ★ origin of gauge symmetry/ quantum numbers
- ★ unification with gravity

The supersymmetry alternative

Supersymmetry: bosons \Leftrightarrow fermions

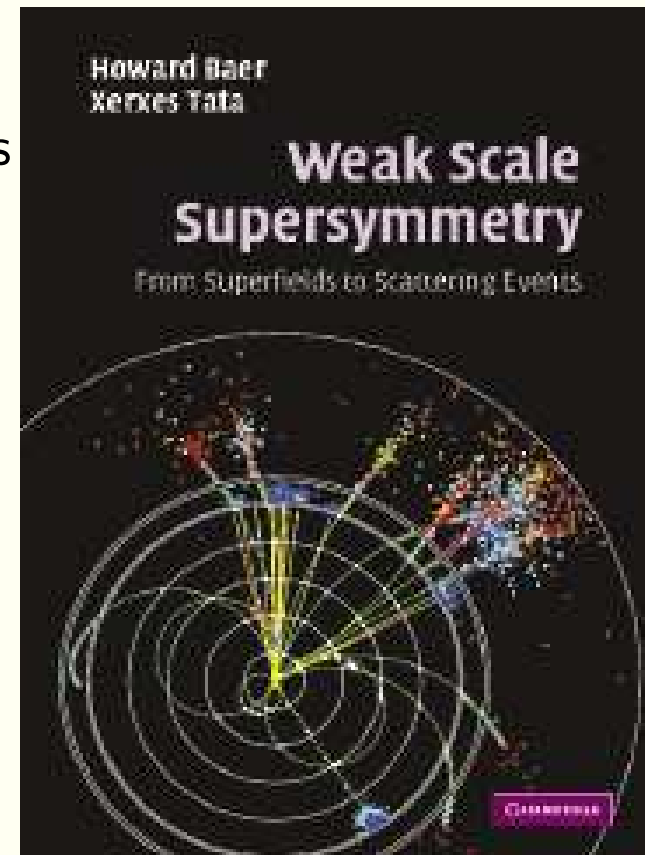
- ★ SUSY is a *space-time* symmetry!
- ★ space-time $x^\mu \Rightarrow (x^\mu, \theta_i)$ $i = 1, \dots, 4$ superspace
- ★ fields $\psi \Rightarrow \hat{\phi} \ni (\phi, \psi)$ superfields
- ★ gauge fields $A^\mu \Rightarrow \hat{W} \ni (\lambda, A^\mu)$ gauge superfields
- ★ superfield formalism \Rightarrow general form for Lagrangian of (globally) supersymmetric gauge theory: quadratic divergences cancel!
- ★ SUSY can be broken by *soft* SUSY breaking terms: maintain cancellation of quadratic divergences

Weak Scale Supersymmetry

HB and X. Tata

Spring, 2006; Cambridge University Press

- ★ Part 1: superfields/Lagrangians
 - 4-component spinor notation for exp'ts
 - master Lagrangian for SUSY gauge theories
- ★ Part 2: models/implications
 - MSSM, SUGRA, GMSB, AMSB, ...
 - dark matter density/detection
- ★ Part 3: SUSY at colliders
 - production/decay/event generation
 - collider signatures
 - R -parity violation



Minimal Supersymmetric Standard Model (MSSM)

- ★ Adopt gauge symmetry of Standard Model
 - spin $\frac{1}{2}$ gaugino for each SM gauge boson
- ★ SM fermions \in chiral scalar superfields: \Rightarrow scalar partner for each SM fermion helicity state
 - electron $\Leftrightarrow \tilde{e}_L$ and \tilde{e}_R
- ★ *two* Higgs doublets to cancel triangle anomalies
- ★ add all admissible soft SUSY breaking terms
- ★ resultant Lagrangian has 124 parameters!
- ★ Lagrangian yields mass eigenstates, mixings, Feynman rules for scattering and decay processes
- ★ predictive model!

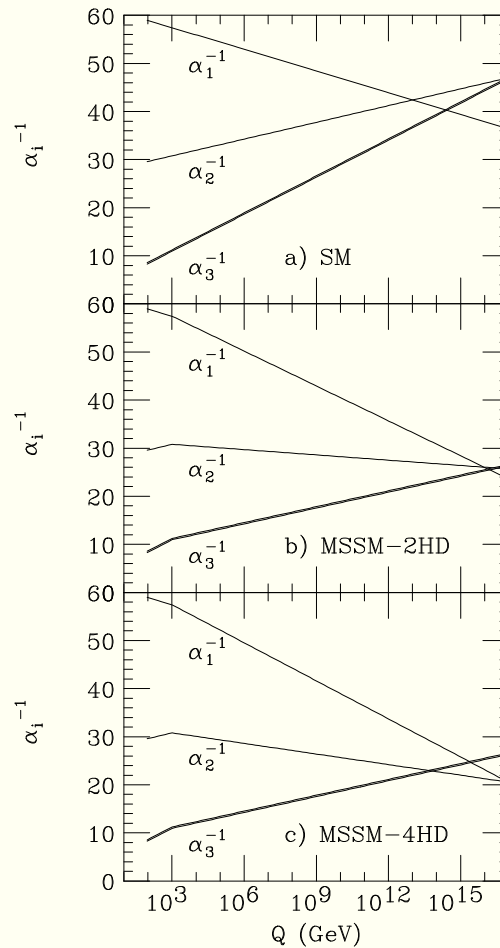
Supergravity (SUGRA)

- ★ $e^{i\bar{\alpha}Q}$ with $\alpha(x)$: *local* SUSY transformation
 - forces introduction of spin 2 graviton and spin $\frac{3}{2}$ gravitino
 - resultant theory \Rightarrow General Relativity in classical limit!
- ★ rules for Lagrangian in supergravity gauge theory: Cremmer et al. (1983)
- ★ fertile ground: supergravity \cup grand unification: LE limit of superstring?
- ★ minimal supergravity model (mSUGRA)
- ★ $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - m_0 = mass of all scalars at $Q = M_{GUT}$
 - $m_{1/2}$ = mass of all gauginos at $Q = M_{GUT}$
 - A_0 = trilinear soft breaking parameter at $Q = M_{GUT}$
 - $\tan\beta$ = ratio of Higgs vevs
 - μ = SUSY Higgs mass term; magnitude determined by REWSB!

Some successes of SUSY GUT theories

- ★ SUSY divergence cancellation maintains hierarchy between GUT scale $Q = 10^{16}$ GeV and weak scale $Q = 100$ GeV
- ★ gauge coupling unification!

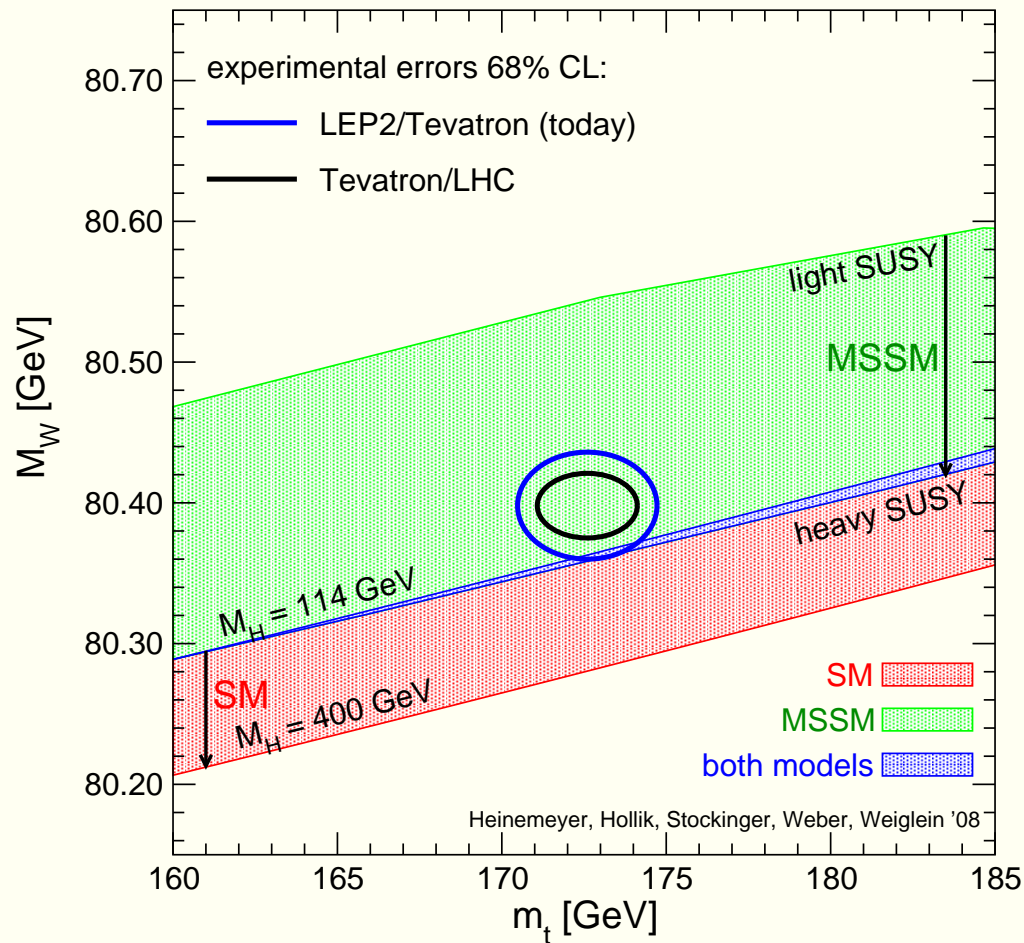
Gauge coupling evolution



Some successes of SUSY GUT theories

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- ★ Lightest Higgs mass $m_h \lesssim 135$ GeV as indicated by radiative corrections!

Precision electroweak data and the Higgs mass:

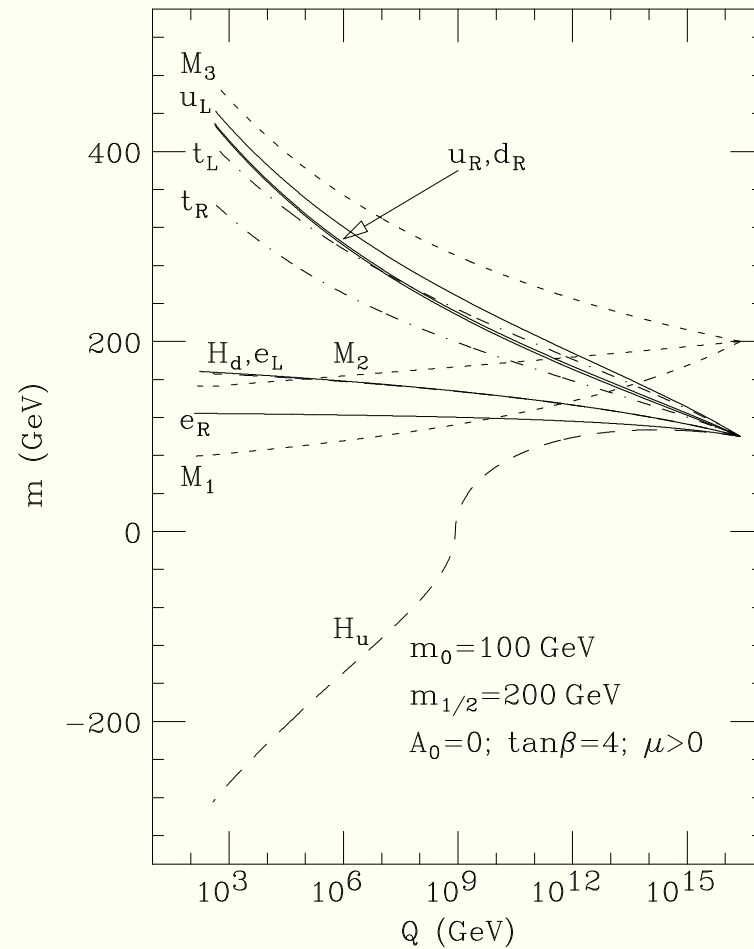


S. Heinemeyer et al.

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- ★ radiative breaking of EW symmetry if $m_t \sim 100 - 200$ GeV!

Soft term evolution and radiative EWSB

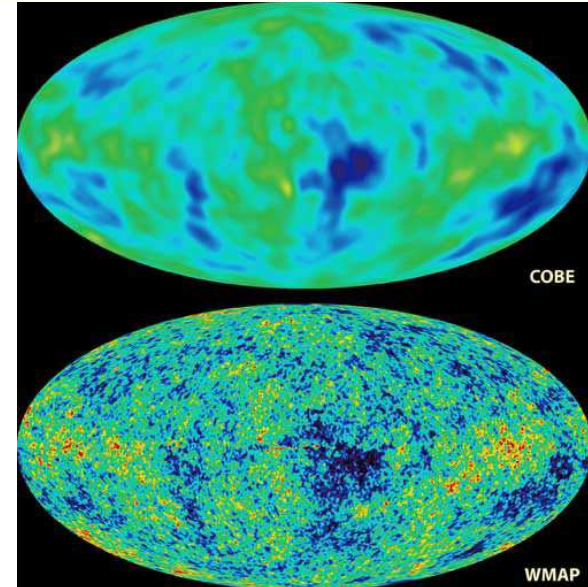


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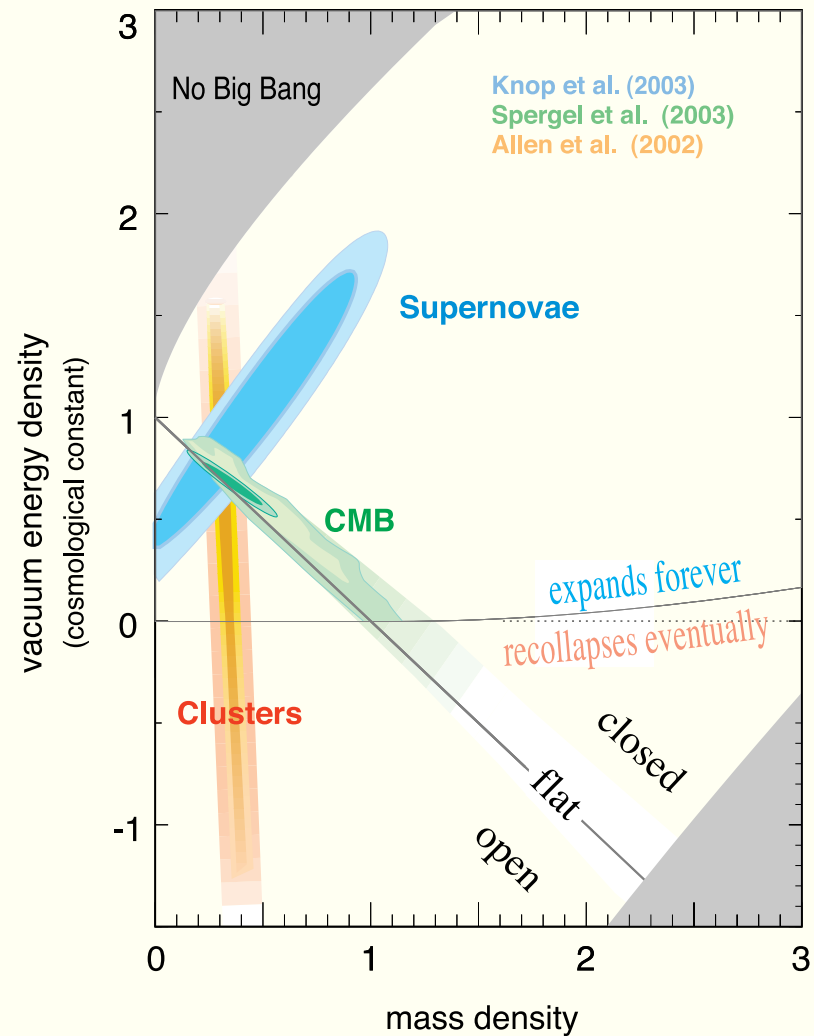
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- ★ radiative breaking of EW symmetry if $m_t \sim 100 - 200$ GeV!
- ★ dark matter candidate: lightest neutralino \tilde{Z}_1
- ★ stabilize neutrino see-saw scale vs. weak scale
- ★ $SO(10)$ SUSY GUT: baryogenesis via leptogenesis
- ★ can give dark energy via CC Λ (but need huge fine-tuning...)
 - SUGRA = low energy limit of superstring?
 - stringy multiverse: anthropic selection of small CC?

Evidence for dark matter in the universe

- ★ binding of galactic clusters (Zwicky, 1930s)
- ★ galactic rotation curves
- ★ large scale structure formation
- ★ inflation $\Rightarrow \Omega = \rho/\rho_c = 1$
- ★ gravitational lensing
- ★ anisotropies in cosmic MB (WMAP)
- ★ surveys of distant galaxies via SN (DE)
- ★ Big Bang nucleosynthesis
 - $\Omega_\Lambda \simeq 0.7$
 - $\Omega_{CDM} \simeq 0.25$
 - $\Omega_{baryons} \simeq 0.045$ (dark baryons ~ 0.040)
 - $\Omega_\nu \sim 0.005$



Dark matter versus dark energy



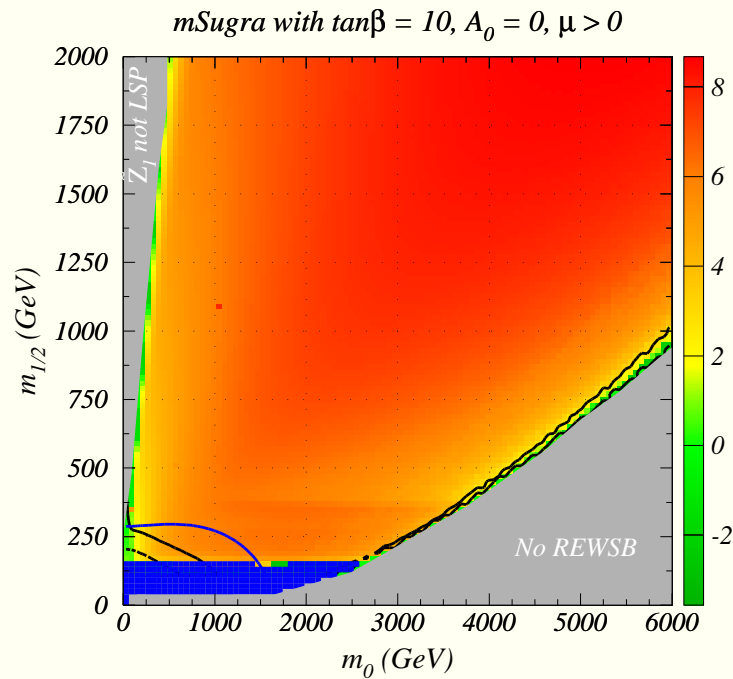
SUSY dark matter

- ★ R-parity conservation \Rightarrow conserved B and $L \Rightarrow$ proton stability
 - $R(\text{particle}) = 1; R(\text{sparticle}) = -1$
- ★ Naturally occurs in $SO(10)$ SUSY GUT theories
- ★ Some consequences:
 - Sparticles are produced in pairs
 - Sparticles decay to other sparticles
 - Lightest SUSY particle (LSP) is absolutely stable (good candidate for dark matter)
- ★ LSP must be charge, color neutral (bound on cosmological relics)
- ★ Sneutrino would have been detected in direct detection experiments
- ★ lightest neutralino \tilde{Z}_1 is LSP in wide range of models
- ★ \tilde{Z}_1 is weakly interacting, massive particle (WIMP)

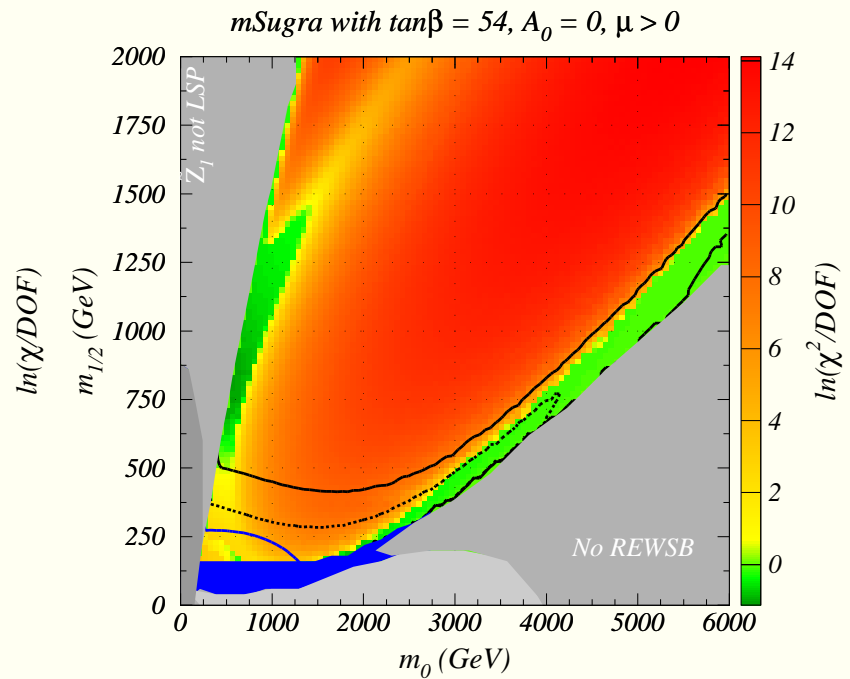
Calculating the relic density of neutralinos

- ★ At very high T , neutralinos in thermal equilibrium with cosmic soup
- ★ As universe expands and cools, expansion rate exceeds interaction rate (freeze-out)
- ★ number density is governed by Boltzmann eq. for FRW universe
 - $dn/dt = -3Hn - \langle\sigma v_{rel}\rangle(n^2 - n_0^2)$
 - $\Omega_{\tilde{Z}_1} h^2 = \frac{s_0}{\rho_c/h^2} \left(\frac{45}{\pi g_*}\right)^{1/2} \frac{x_f}{m_{Pl}} \frac{1}{\langle\sigma v\rangle}$
 - $\Omega_{CDM} h^2 \sim 0.1 \Rightarrow \langle\sigma v\rangle \sim 0.9 \text{ pb!}$
 - $\langle\sigma v\rangle = \pi\alpha^2/8m^2 \Rightarrow m \sim 100 \text{ GeV}$
 - “The WIMP miracle!”: cosmic motivation for new physics at weak scale
- ★ SUSY: 1722 annihilation/co-annihilation reactions; 7618 Feynman diagrams
- ★ IsaReD program (HB, A. Belyaev , C. Balazs)

Results of χ^2 fit using τ data for a_μ :



— $m_h = 114.1 \text{ GeV}$ ■ LEP2 excluded
 — SuperCDMS CDMSII CDMS

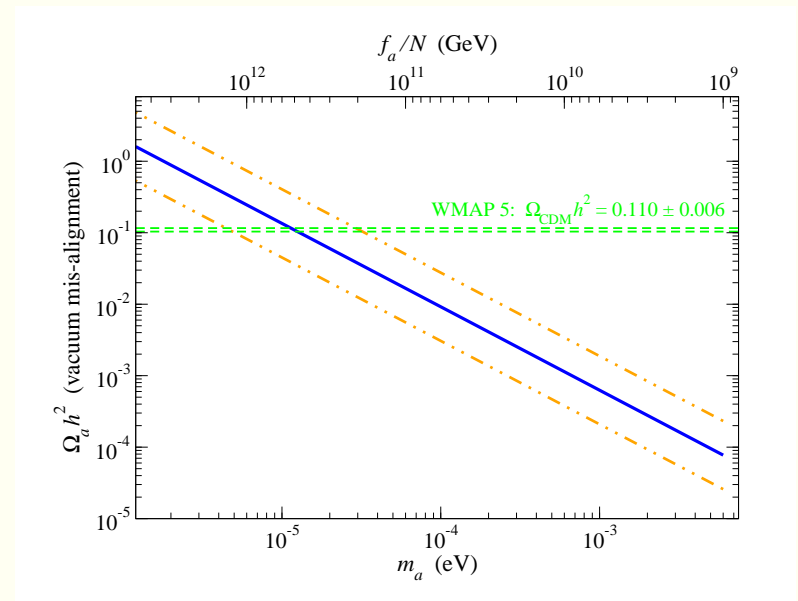


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HB, C. Balazs: JCAP 0305, 006 (2003)

Axions

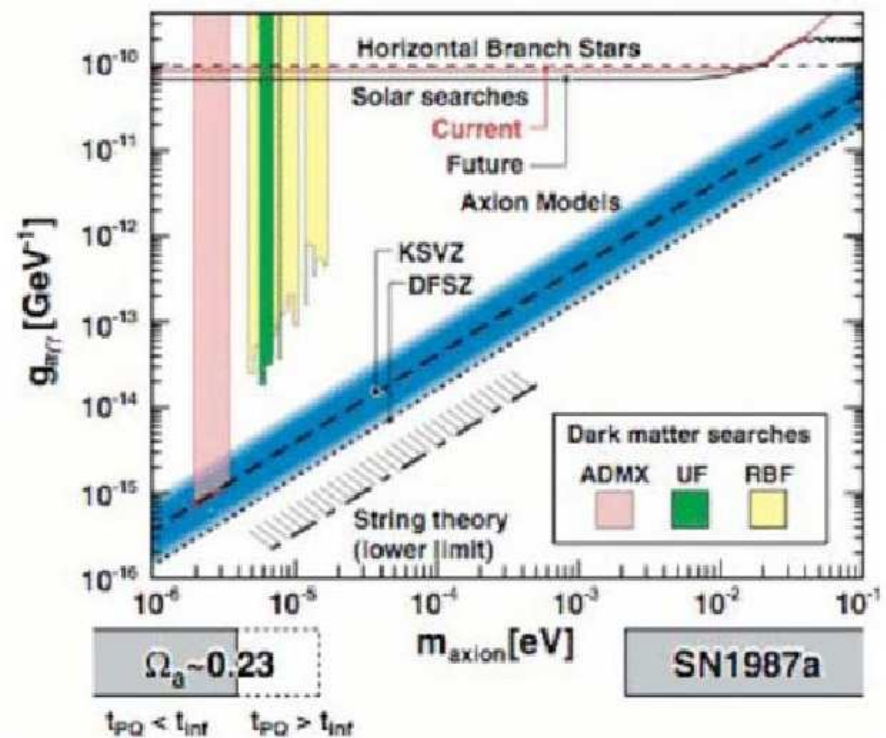
- ★ PQ solution to strong CP problem in QCD
- ★ pseudo-Goldstone boson from PQ breaking at scale $f_a \sim 10^9 - 10^{12}$ GeV
- ★ non-thermally produced via vacuum mis-alignment as *cold* DM
 - $m_a \sim \Lambda_{QCD}^2 / f_a \sim 10^{-6} - 10^{-1} eV$
 - $\Omega_a h^2 \sim \frac{1}{2} \left[\frac{6 \times 10^{-6} eV}{m_a} \right]^{7/6} h^2$
 - astro bound: stellar cooling $\Rightarrow m_a < 10^{-1} eV$
 - a couples to EM field: $a - \gamma - \gamma$ coupling (Sikivie)
 - axion microwave cavity searches



Axion microwave cavity searches

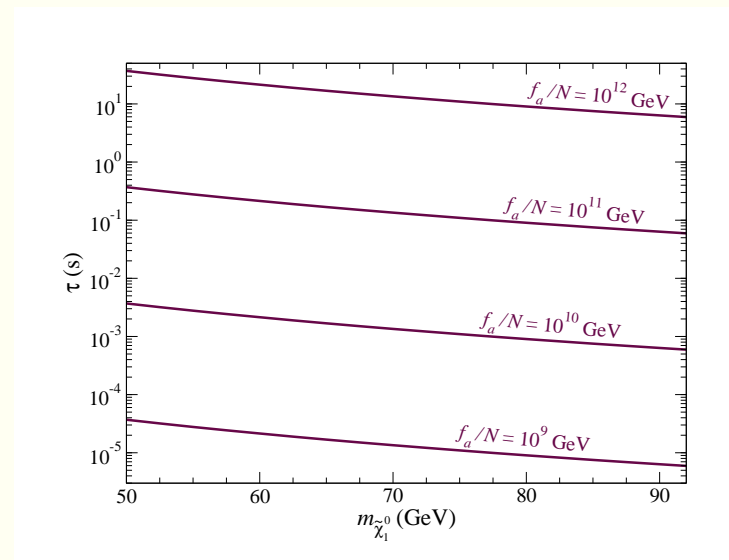
★ ongoing searches: ADMX experiment

- Livermore \Rightarrow U Wash.
- Phase I: probe KSVZ
for $m_a \sim 10^{-6} - 10^{-5} \text{ eV}$
- Phase II: probe DFSZ
for $m_a \sim 10^{-6} - 10^{-5} \text{ eV}$
- beyond Phase II:
probe higher values m_a



Axions + SUSY \Rightarrow Axino \tilde{a} dark matter

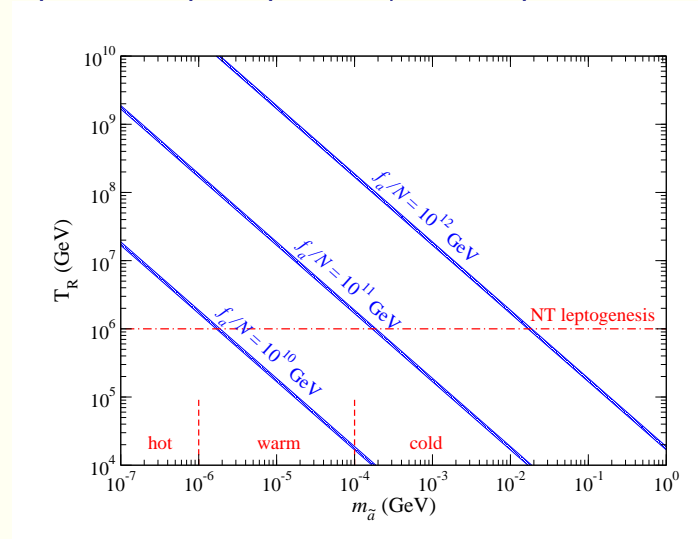
- axino is spin- $\frac{1}{2}$ element of axion supermultiplet (R -odd; can be LSP)
- $m_{\tilde{a}}$ model dependent: keV \rightarrow GeV
- $\tilde{Z}_1 \rightarrow \tilde{a}\gamma$
- non-thermal \tilde{a} production via \tilde{Z}_1 decay:
- axinos inherit neutralino number density
- $\Omega_{\tilde{a}}^{NTP} h^2 = \frac{m_{\tilde{a}}}{m_{\tilde{Z}_1}} \Omega_{\tilde{Z}_1} h^2$:



Thermally produced axinos

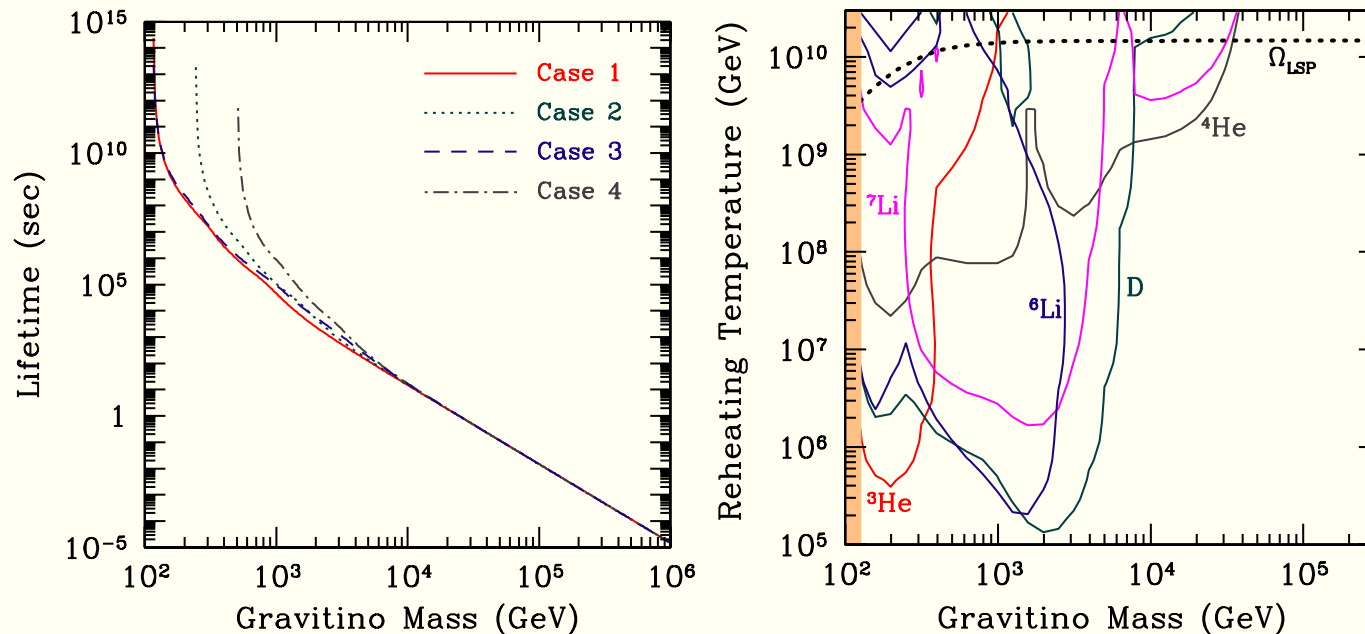
- ★ If $T_R < f_a$, then axinos never in thermal equilibrium in early universe
- ★ Can still produce \tilde{a} thermally via radiation off particles in thermal equilibrium
- ★ Brandenberg-Steffen calculation:

$$\Omega_{\tilde{a}}^{TP} h^2 \simeq 5.5 g_s^6 \ln \left(\frac{1.108}{g_s} \right) \left(\frac{10^{11} \text{ GeV}}{f_a/N} \right)^2 \left(\frac{m_{\tilde{a}}}{0.1 \text{ GeV}} \right) \left(\frac{T_R}{10^4 \text{ GeV}} \right) \quad (3)$$



Gravitinos: spin- $\frac{3}{2}$ partner of graviton

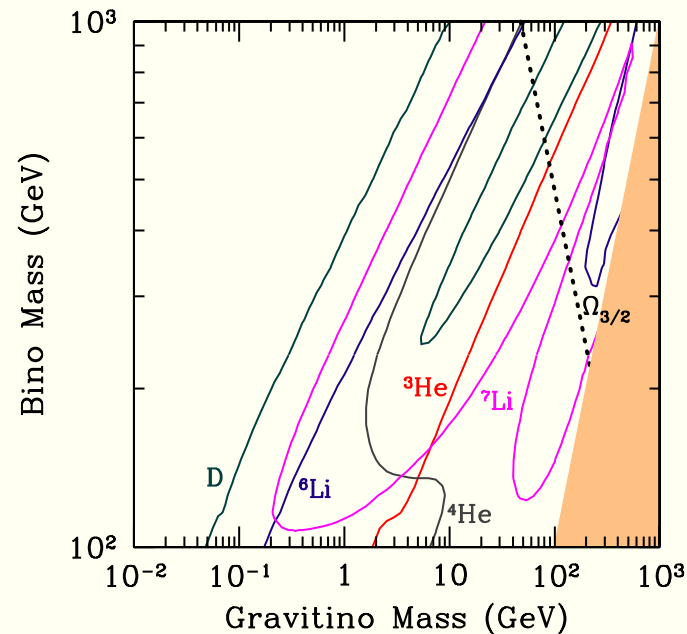
- gravitino problem in generic SUGRA models: overproduction of \tilde{G} followed by late \tilde{G} decay can destroy successful BBN predictions: upper bound on T_R



(see Kawasaki, Kohri, Moroi, Yotsuyanagi; Cybert, Ellis, Fields, Olive)

Gravitinos as dark matter: again the gravitino problem

- neutralino production in generic SUGRA models: followed by late time $\tilde{Z}_1 \rightarrow \tilde{G} + X$ decays can destroy successful BBN predictions:

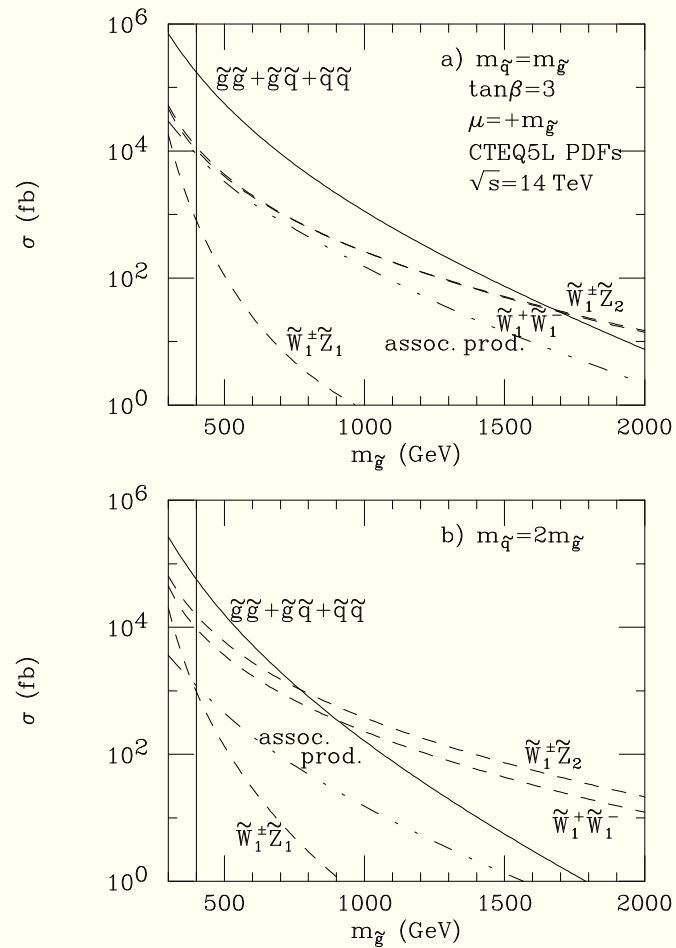


(see Kawasaki, Kohri, Moroi, Yotsuyanagi)

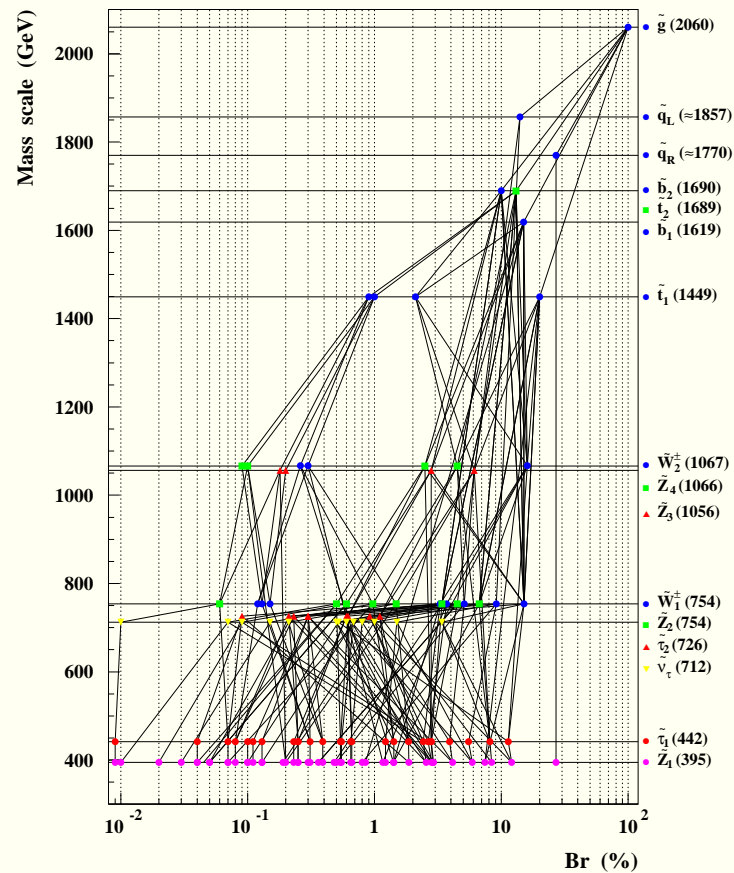
Gravitino dark matter: if one can avoid gravitino problem

- ★ $m_{\tilde{G}} = F/\sqrt{3}M_* \sim \text{TeV}$ in Supergravity models
 - if \tilde{G} is LSP, then calculate NLSP abundance as a thermal relic: $\Omega_{NLSP} h^2$
 - $\tilde{Z}_1 \rightarrow h\tilde{G}$, $Z\tilde{G}$, $\gamma\tilde{G}$ or $\tilde{\tau}_1 \rightarrow \tau\tilde{G}$ possible
 - * lifetime $\tau_{NLSP} \sim 10^4 - 10^8$ sec
 - * also produce \tilde{G} thermally (depends on re-heat temp. T_R)
 - * DM relic density is then $\Omega_{\tilde{G}} = \frac{m_{\tilde{G}}}{m_{NLSP}} \Omega_{NLSP} + \Omega_{\tilde{G}}^{TP}$
 - * Feng et al.; Ellis et al.; Brandenberg+Steffen; Buchmuller et al.
 - \tilde{G} undetectable via direct/indirect DM searches
 - unique collider signatures are possible:
 - * $\tilde{\tau}_1 = \text{NLSP}$: stable charged tracks
 - * can collect NLSPs in e.g. water (slepton trapping)
 - * monitor for $NLSP \rightarrow \tilde{G}$ decays

Production of sparticles at CERN LHC

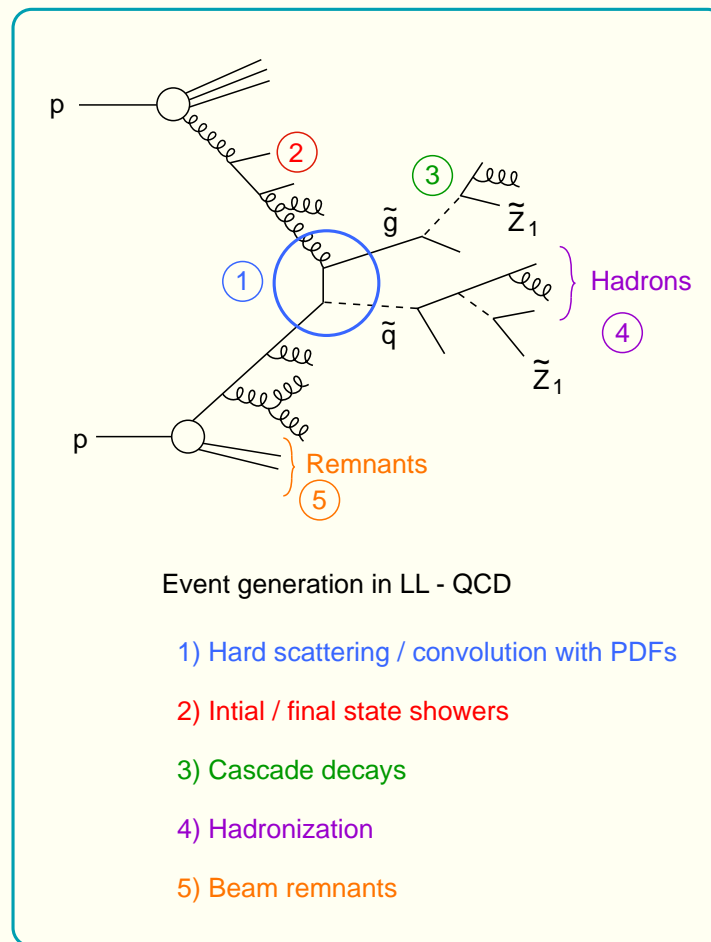


Sparticle cascade decays



\tilde{Z}_4 qq (27.0 %)	\tilde{Z}_4 ν WWbb (4.1 %)
\tilde{Z}_4 τ Wbb (12.1 %)	\tilde{Z}_4 τ bb (2.9 %)
\tilde{Z}_4 τ τ Wbb (8.4 %)	\tilde{Z}_4 τ qq (2.9 %)
\tilde{Z}_4 WWbb (7.4 %)	\tilde{Z}_4 τ ZWbb (2.8 %)
\tilde{Z}_4 τ qq (5.9 %)	\tilde{Z}_4 τ hWbb (2.6 %)

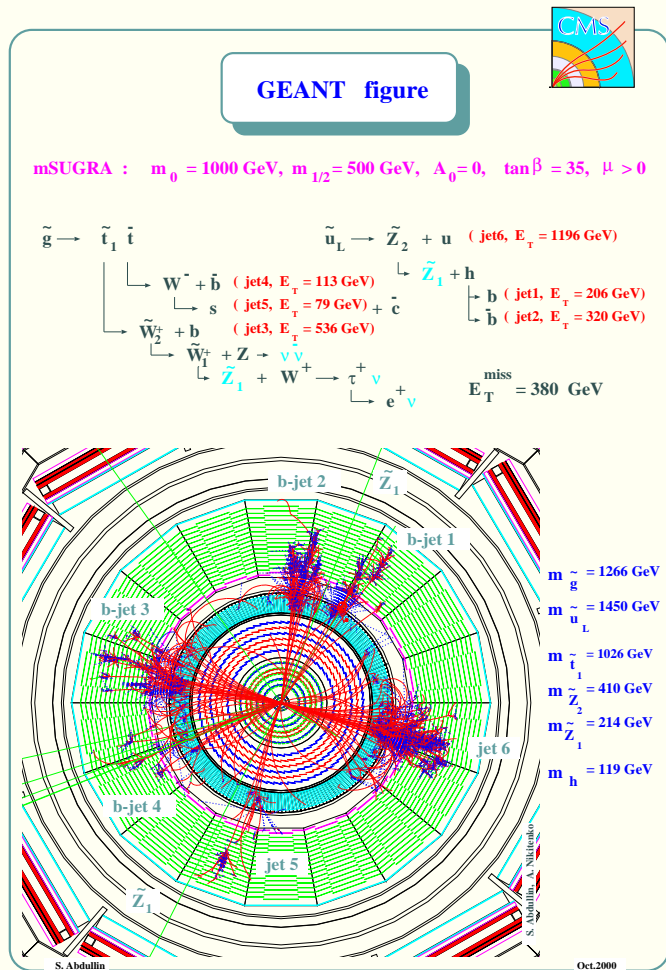
Event generation for sparticles



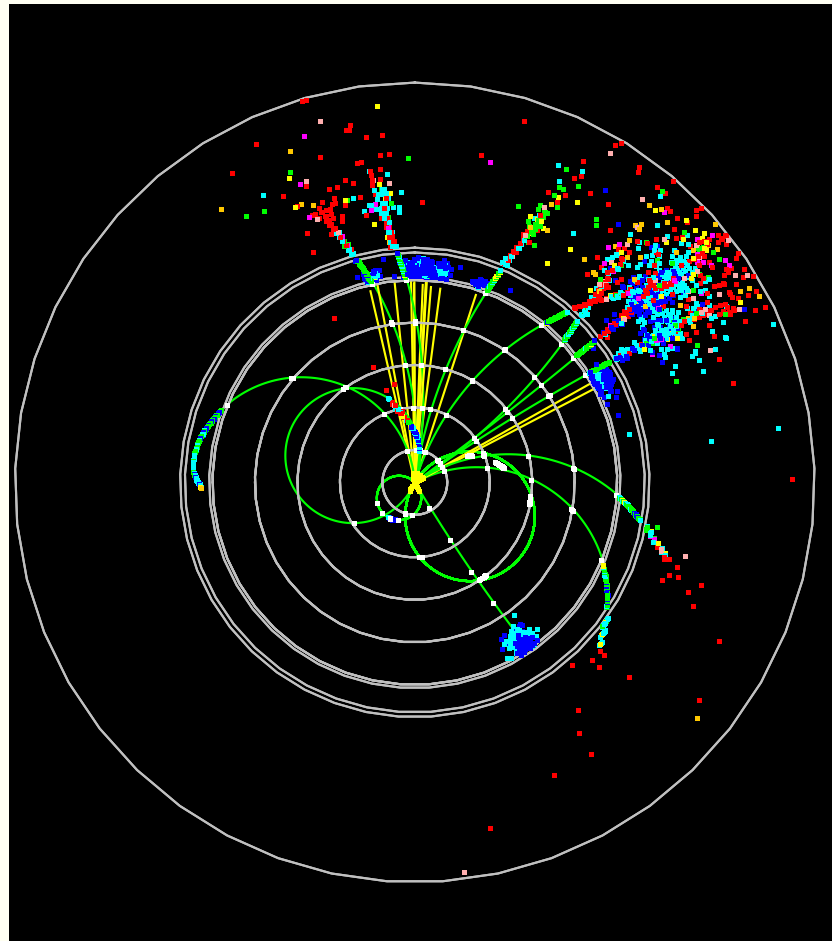
Isajet v7.79 for sparticle event generation

- ★ Isajet (1979), by F. Paige and S. Protopopescu
- ★ Isajet 7.0 (1993) -7.75: FP, SP, HB and X. Tata
 - Isasugra subprogram: SUGRA models (and others) \Rightarrow sparticle masses, mixings, decay rates
- ★ SUSY and SM event generation for hadron colliders
- ★ e^+e^- colliders
 - polarized beams
 - bremsstrahlung/ beamstrahlung
- ★ IsaTools: $\Omega_{\tilde{Z}_1} h^2$, $(g-2)_\mu$, $BF(b \rightarrow s\gamma)$, $BF(B_s \rightarrow \mu^+\mu^-)$, $\sigma(\tilde{Z}_1 p)$
- ★ Les Houches event output: 7.78

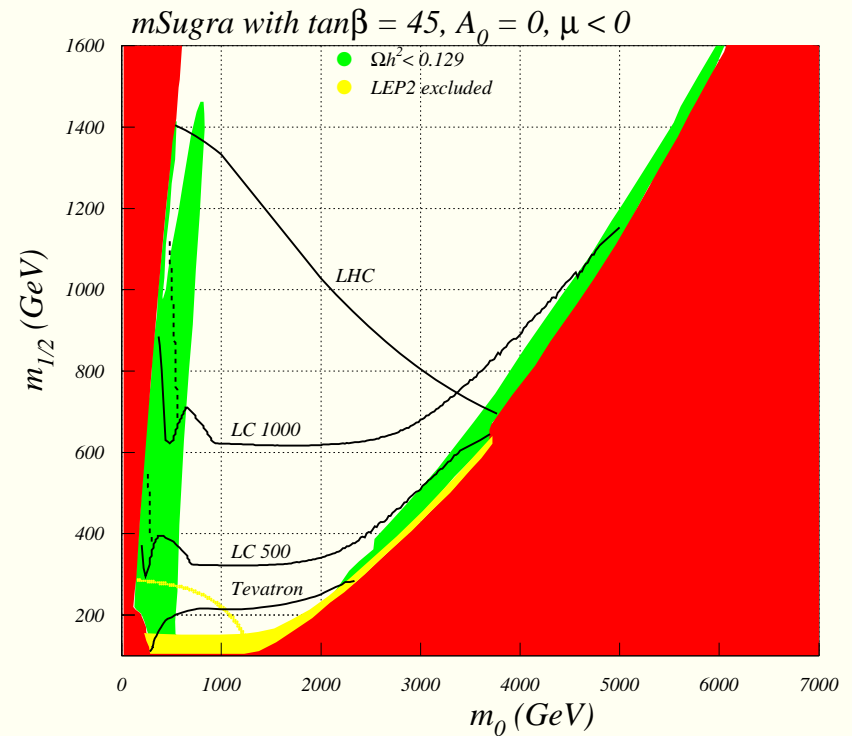
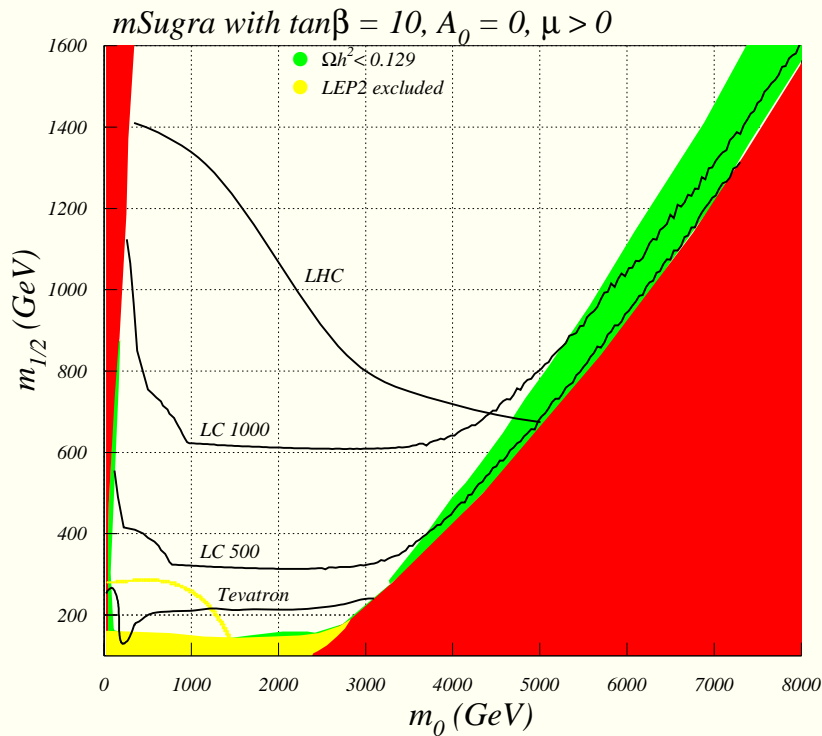
Simulated sparticle production event at LHC



$e^+e^- \rightarrow \widetilde{W}_1^+ \widetilde{W}_1^- \rightarrow (q\bar{q}' \widetilde{Z}_1) + (e\bar{\nu}_e \widetilde{Z}_1)$ at linear collider



Sparticle reach of all colliders with relic density

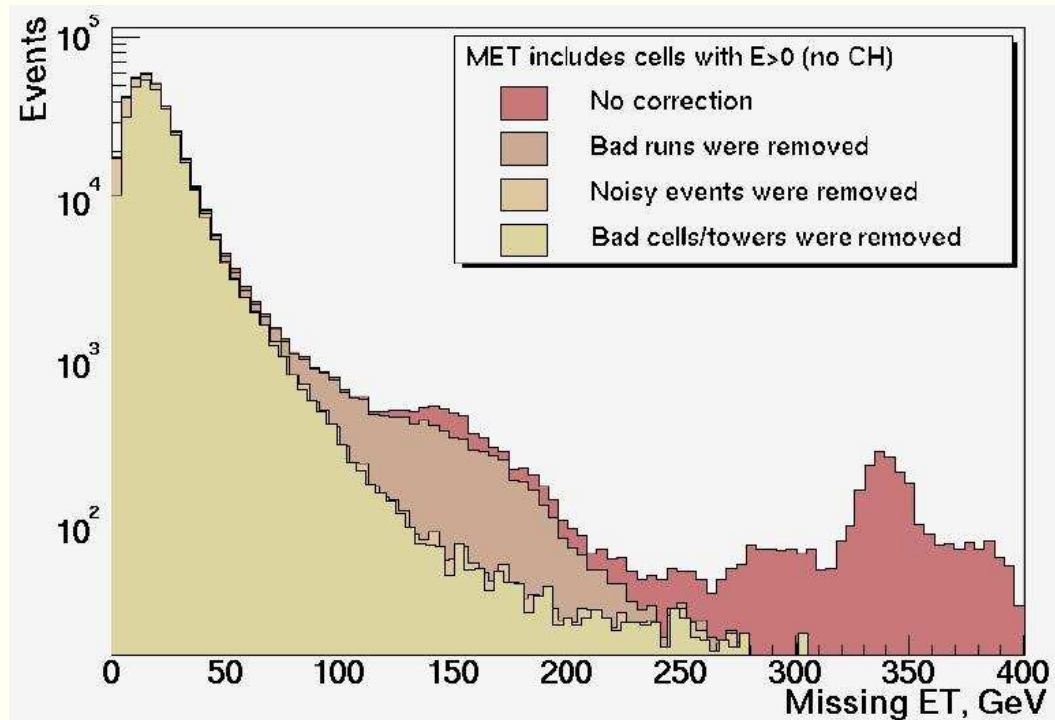


HB, Belyaev, Krupovnickas, Tata: JHEP 0402, 007 (2004)

Early SUSY discovery at LHC with just 0.1 fb^{-1} ?

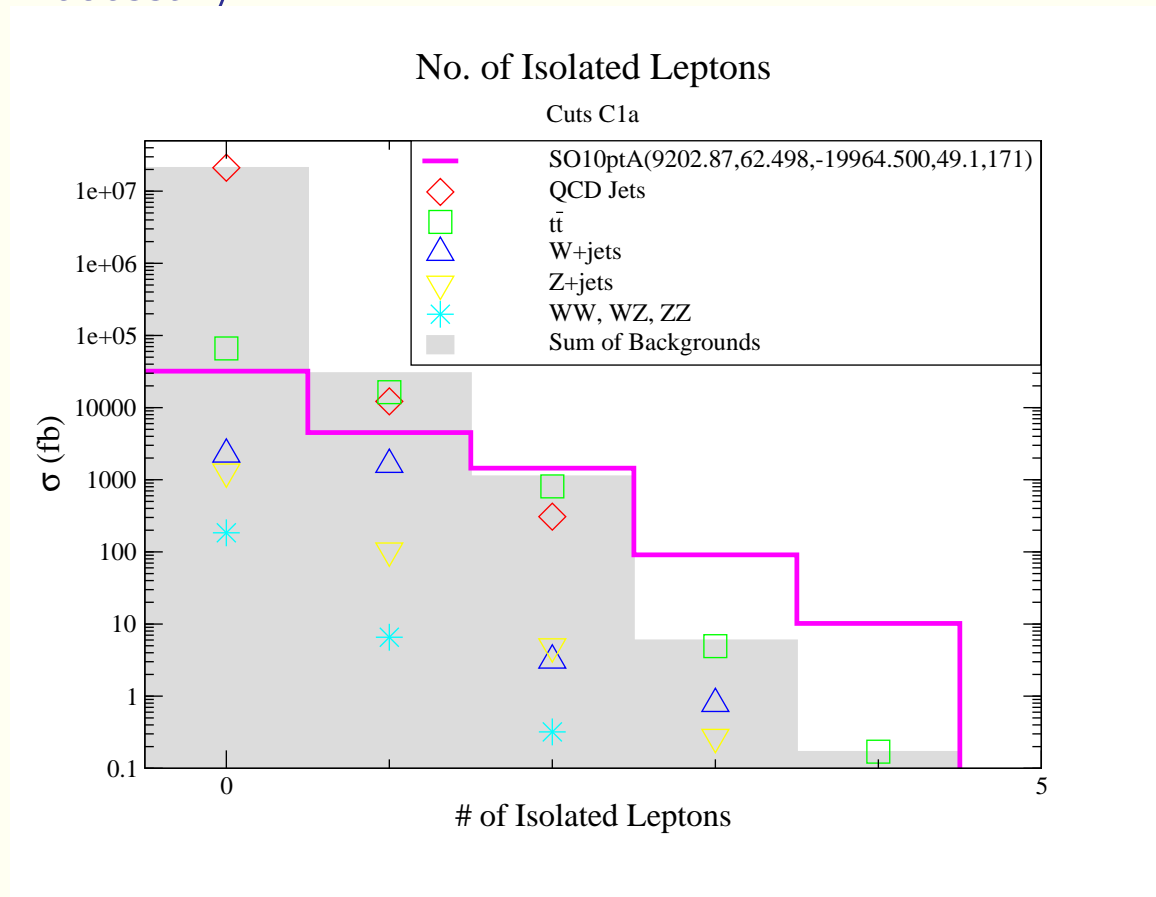
- To make \cancel{E}_T cut, complete knowledge of detector needed
 - dead regions
 - “hot” cells
 - cosmic rays
 - calorimeter mis-measurement
 - beam-gas events
- Can we make early discovery of SUSY at LHC *without* \cancel{E}_T ?
- Expect SUSY events to be rich in jets, b -jets, isolated ℓ s, τ -jets,....
- These are *detectable*, rather than inferred objects
- Answer: YES! See HB, Prosper, Summy, arXiv:0801.3799

D0 saga with missing E_T

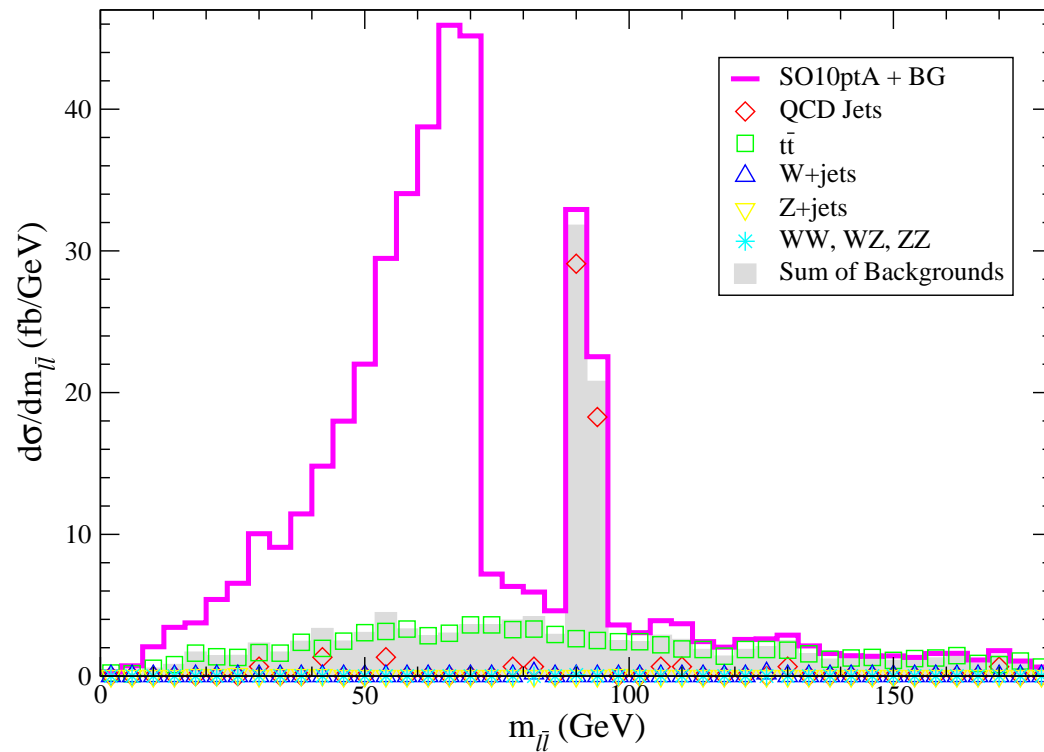


Simple cuts: ≥ 4 jets plus isolated leptons

- \cancel{E}_T not really necessary



Cuts C1' plus ≥ 2 OS/SF ℓ



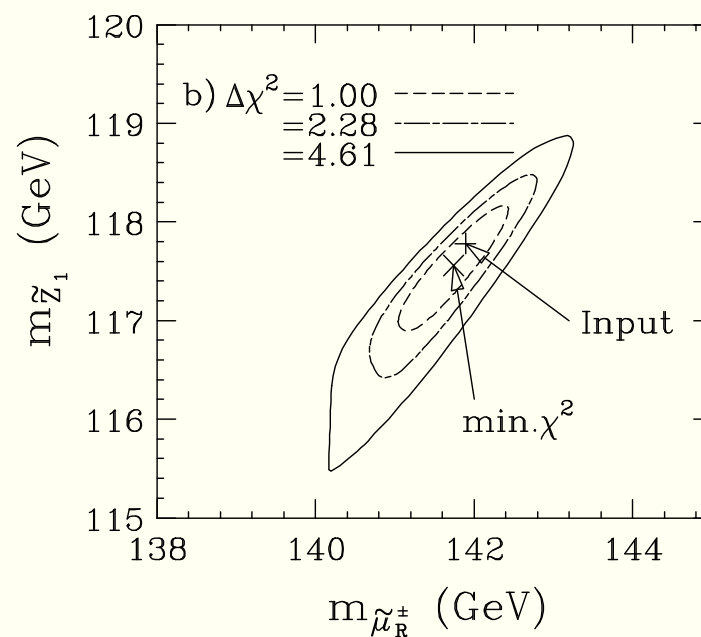
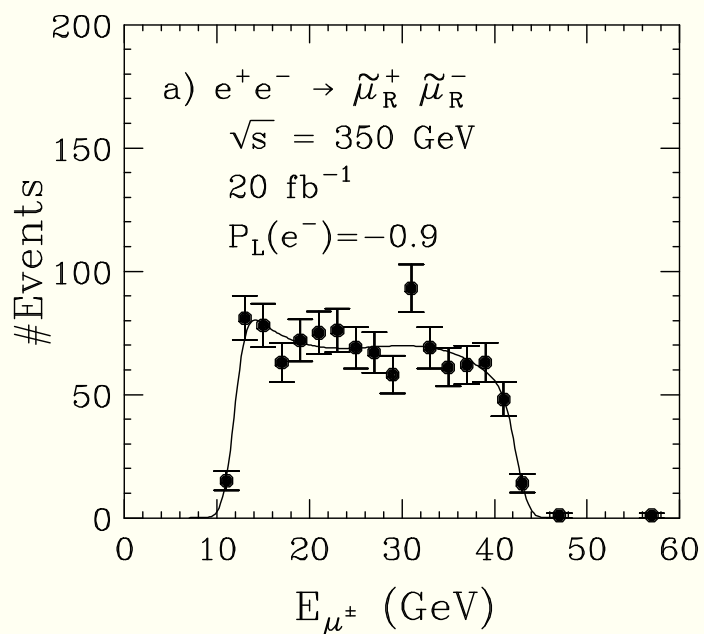
Precision measurements at LHC: Atlas and CMS

- $M_{eff} = \cancel{E}_T + E_T(j1) + \dots + E_T(j4)$ sets overall $m_{\tilde{g}}, m_{\tilde{q}}$ scale
- $m(\ell\bar{\ell}) < m_{\tilde{Z}_2} - m_{\tilde{Z}_1}$ mass edge
- $m(\ell\bar{\ell})$ distribution shape
- combine $m(\ell\bar{\ell})$ with jets to gain $m(\ell\bar{\ell}j)$ mass edge: info on $m_{\tilde{q}}$
- further mass edges possible *e.g.* $m(\ell\bar{\ell}jj)$
- Higgs mass bump $h \rightarrow b\bar{b}$ likely visible in $\cancel{E}_T + jets$ events
- in favorable cases, may overconstrain system for a given model
- ★ methodology very p-space dependent
- ★ some regions are very difficult *e.g.* HB/FP

International linear e^+e^- collider (ILC)

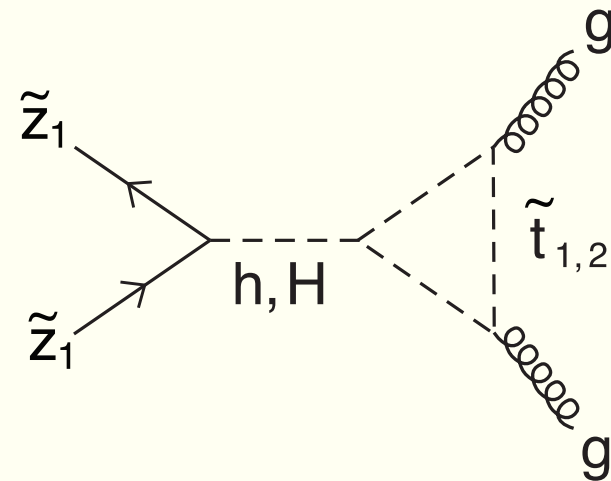
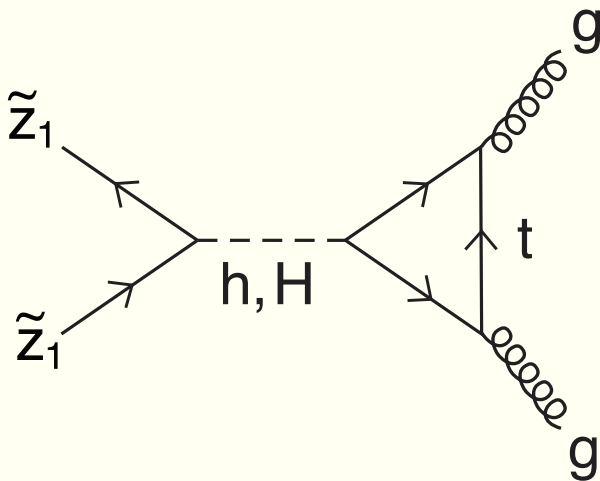
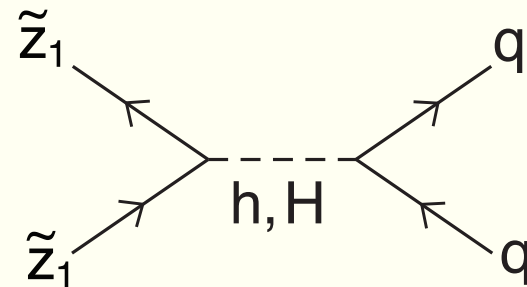
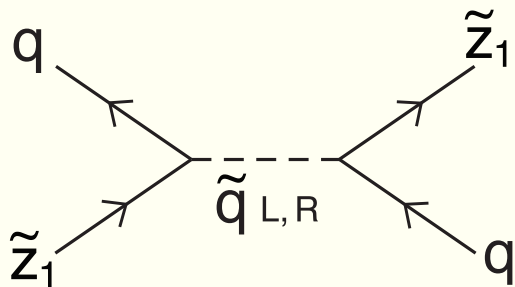
- ★ A linear e^+e^- collider with $\sqrt{s} = 0.5 - 1$ TeV is highest priority project for HEP beyond LHC! Why?
 - All beam energy \Rightarrow collision (aside from brem/beamstrahlung losses)
 - beam energy known
 - clean collision environment
 - low (electroweak) background levels
 - adjustable beam energy (threshold scans)
 - e^- and possibly e^+ beam polarization
- ★ ILC will be *ideal* machine to perform precision spectroscopy of any new (EW interacting) matter states (provided they are kinematically accessible)!
- ★ timeline: decision-2012; ready-2025?

Precision sparticle measurements at a e^+e^- linear collider

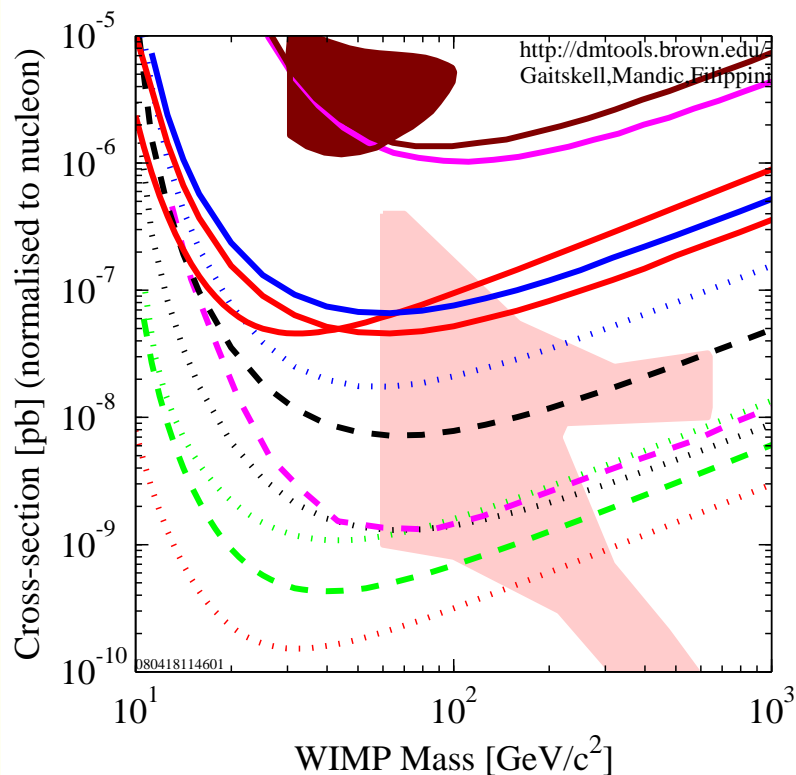


Direct detection of SUSY DM

★ Direct search via neutralino-nucleon scattering



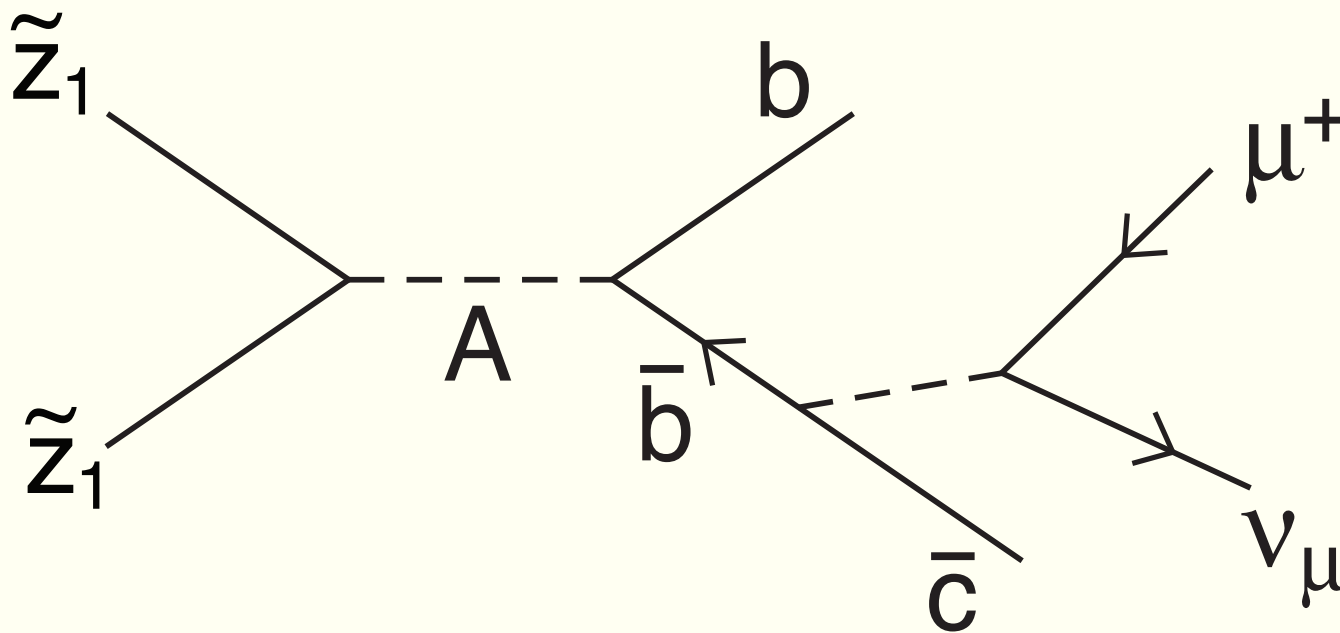
Direct detection of neutralino DM: the race is on!



- DATA listed top to bottom on plot
- Edelweiss I final limit, 62 kg-days Ge 2000+2002+2003 limit
 - DAMA 2000 58k kg-days NaI Ann. Mod. 3sigma w/DAMA 1996
 - WARP 2.3L, 96.5 kg-days 55 keV threshold
 - CDMS 2008 Ge
 - CDMS: 2004+2005 (reanalysis) +2008 Ge
 - XENON10 2007 (Net 136 kg-d)
 - CDMS Soudan 2007 projected
 - SuperCDMS (Projected) 2-ST@Soudan
 - WARP 140kg (proj)
 - SuperCDMS (Projected) 25kg (7-ST@Snolab)
 - XENON100 (150 kg) projected sensitivity
 - LUX 300 kg LXe Projection (Jul 2007)
 - XENON1T (proj)
 - Baer et. al 2003
- 080418114601

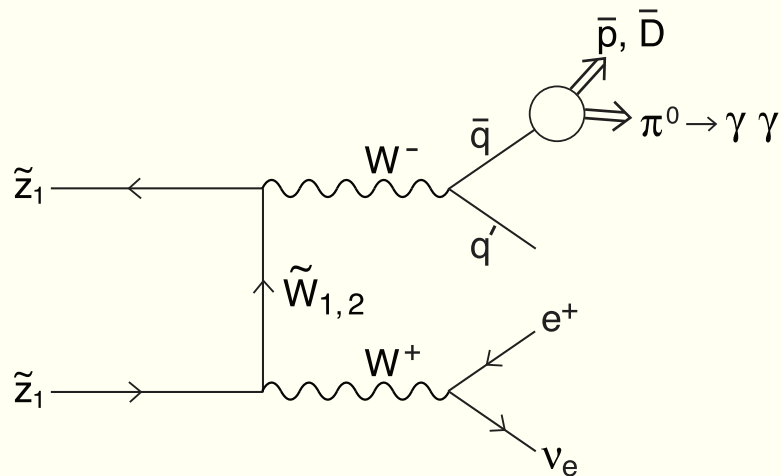
Indirect detection (ID) of SUSY DM: ν -telescopes

- ★ $\tilde{Z}_1 \tilde{Z}_1 \rightarrow b\bar{b}$, etc. in core of sun (or earth): $\Rightarrow \nu_\mu \rightarrow \mu$ in ν telescopes
 - Amanda, Icecube, Antares

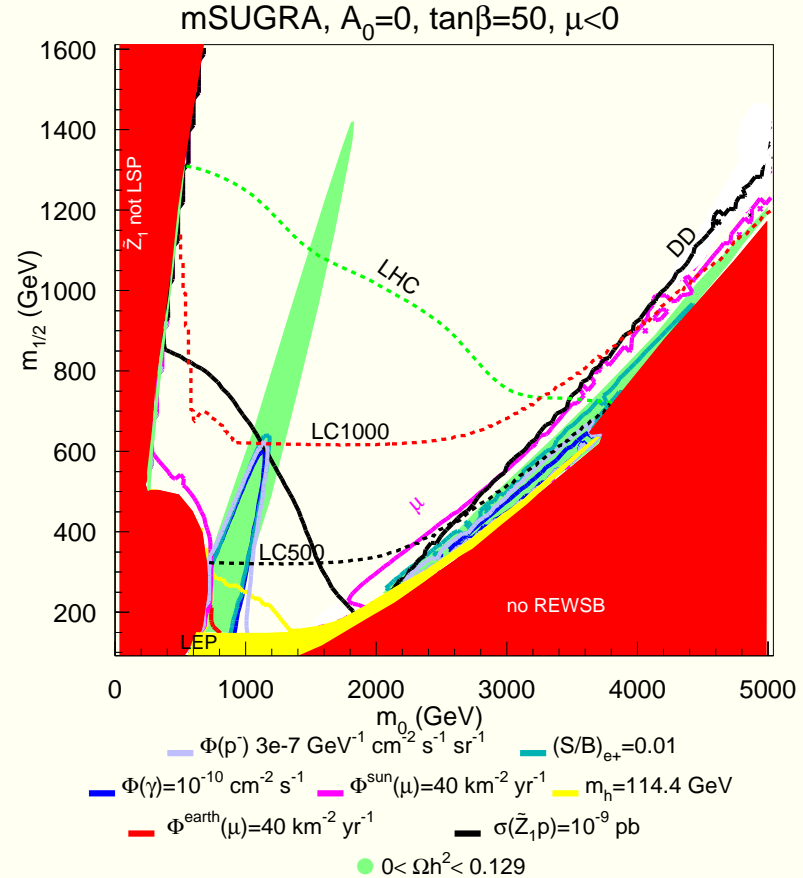
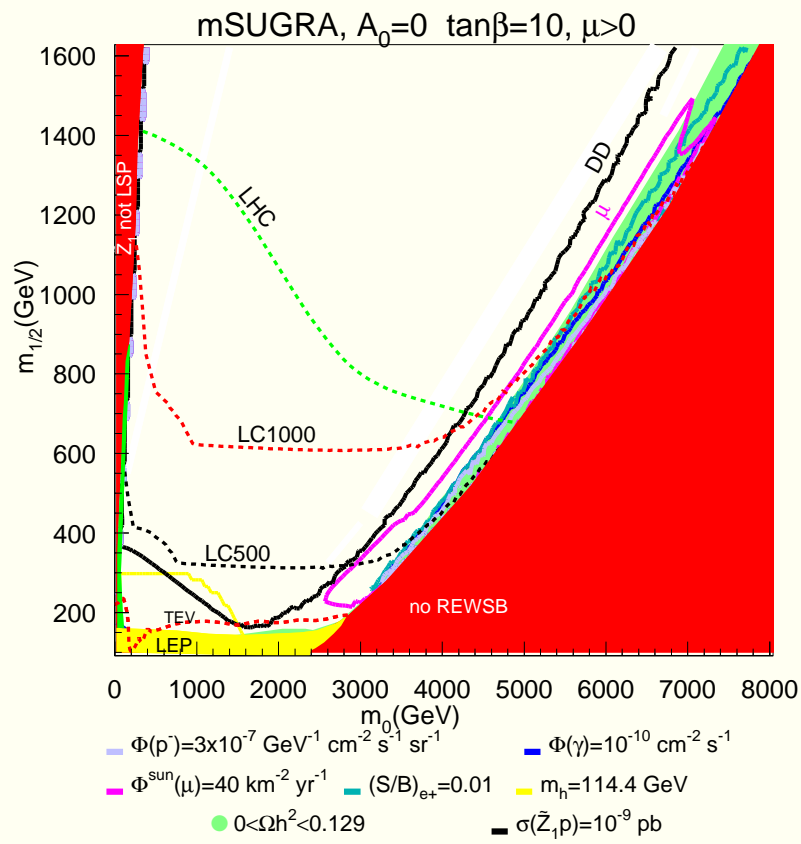


ID of SUSY DM: γ and anti-matter searches

- $\tilde{Z}_1 \tilde{Z}_1 \rightarrow q\bar{q}, \text{etc.} \rightarrow \gamma$ in galactic core or halo
- $\tilde{Z}_1 \tilde{Z}_1 \rightarrow q\bar{q}, \text{etc.} \rightarrow e^+$ in galactic halo
- $\tilde{Z}_1 \tilde{Z}_1 \rightarrow q\bar{q}, \text{etc.} \rightarrow \bar{p}$ in galactic halo
- $\tilde{Z}_1 \tilde{Z}_1 \rightarrow q\bar{q}, \text{etc.} \rightarrow \bar{D}$ in galactic halo



Direct and indirect detection of neutralino DM



HB, Belyaev, Krupovnickas, O'Farrill: JCAP 0408, 005 (2004)

Impact of DM direct/indirect detection on LHC program

- Extend reach in $\sigma_{SI} \sim 10^{-9} - 10^{-10}$ pb
 - explore thoroughly region of MHDM, possibly MWDM
- after discovery, extract m_{wimp} ?
 - $m_{\tilde{Z}_1}$ sets absolute mass scale for SUSY particles-
 - combine with LHC mass edges to gain LHC absolute sparticle masses
 - learn if \tilde{Z}_1 is absolutely stable: R -conservation
- IceCube turn-on can discover/verify especially MHDM
- knowledge of LHC spectra, σ_{SI} , σ_{SD} combined with possible gamma ray signals may allow map of dark matter distribution in the galaxy
- role of \bar{p} , e^+ , \bar{D} signals

Models beyond mSUGRA

- ★ Normal scalar mass hierarchy
 - split scalar generations $m_0(1) \simeq m_0(2) \ll m_0(3)$
 - resolves $BF(b \rightarrow s\gamma)$ and $(g-2)_\mu$
- ★ Non-universal Higgs scalars
 - motivated by $SO(10)$ and $SU(5)$ SUSY GUTs
 - allow A -funnel at low $\tan\beta$; higgsino DM at low m_0
 - enhanced DD/ID rates
- ★ DM in models with $t-b-\tau$ Yukawa unification ($SO(10)$)
- ★ Mixed wino DM
- ★ Bino-wino co-annihilation (BWCA) DM
- ★ Low M_3 mixed higgsino DM
- ★ KKLT mixed moduli/AMSB DM

Conclusions

- ★ Supersymmetry is very compelling BSM theory
- ★ Irrefragable case for CDM has emerged
- ★ Some reach for SUSY at Tevatron
- ★ Huge reach for SUSY at CERN LHC
- ★ Possible early SUSY discovery at LHC: leptons instead of \cancel{E}_T
- ★ e^+e^- LC necessary for precision sparticle spectroscopy
- ★ Direct search for WIMP/axion DM is underway
- ★ Indirect search for WIMP DM via Icecube ν telescope
- ★ Indirect search via γ , \bar{p} , e^+ , \bar{D} detection from galactic core/halo WIMP annihilations
- ★ Solution of mystery of CDM is near if CDM = lightest SUSY particle!